

Concentration–discharge relationships reflect chemostatic characteristics of US catchments

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Abstract:

Concentration–discharge relationships have been widely used as clues to the hydrochemical processes that control runoff chemistry. Here we examine concentration–discharge relationships for solutes produced primarily by mineral weathering in 59 geochemically diverse US catchments. We show that these catchments exhibit nearly chemostatic behaviour; their stream concentrations of weathering products such as Ca, Mg, Na, and Si typically vary by factors of only 3 to 20 while discharge varies by several orders of magnitude. Similar patterns are observed at the inter-annual time scale. This behaviour implies that solute concentrations in stream water are not determined by simple dilution of a fixed solute flux by a variable flux of water, and that rates of solute production and/or mobilization must be nearly proportional to water fluxes, both on storm and inter-annual timescales. We compared these catchments' concentration–discharge relationships to the predictions of several simple hydrological and geochemical models. Most of these models can be forced to approximately fit the observed concentration–discharge relationships, but often only by assuming unrealistic or internally inconsistent parameter values. We propose a new model that also fits the data and may be more robust. We suggest possible tests of the new model for future studies. The relative stability of concentration under widely varying discharge may help make aquatic environments habitable. It also implies that fluxes of weathering solutes in streams, and thus fluxes of alkalinity to the oceans, are determined primarily by water fluxes. Thus, hydrology may be a major driver of the ocean-alkalinity feedback regulating climate change. Copyright © 2009 John Wiley & Sons, Ltd.

KEY WORDS concentration–discharge; dissolved load; solute; chemical weathering; Hydrologic Benchmark Network; water quality; catchment; watershed

Received 27 August 2008; Accepted 19 February 2009

INTRODUCTION

Chemical weathering and solute transport are coupled with hydrology in catchments, and this coupling is reflected in the relationships between solute concentrations and stream discharge. Catchment hydrologists often study concentration–discharge relationships because the necessary data are frequently available and the initial analysis is straightforward. However, despite decades of work, there are still open questions about what concentration–discharge relationships can tell us about catchment behavior.

Concentrations of the major base cations and silica have generally been observed to decrease with discharge (Hem, 1948, 1985; Johnson *et al.*, 1969 and references therein; Waylen, 1979; Walling and Webb, 1986; Clow and Drever, 1996). Typical concentration–discharge analyses have centered on mixing models of different source waters (e.g. event and pre-event water; old and new water; or soil water, groundwater and precipitation)

inferred from the shape of the concentration–discharge relationship for different solutes (Johnson *et al.*, 1969; Hall, 1970, 1971). In other studies, researchers have inferred the relative timing of mixing from hysteresis loops observed in concentration–discharge plots (Evans and Davies, 1998; Evans *et al.*, 1999; House and Warwick, 1998; Hornberger *et al.*, 2001; Chanut *et al.*, 2002). Evans and Davies (1998) proposed that the form and direction of hysteresis loops could uniquely identify the rank order of end-member concentrations in a three end-member mixing scenario. However, Chanut *et al.* (2002) showed that even the small number of assumptions required for this identification are not always valid, and that when the assumptions are violated, hysteresis loops cannot definitively distinguish the relative concentrations of different end-members. Nonetheless, other characteristics of concentration–discharge relationships may provide insight into the coupling of chemical weathering and hydrological processes in catchments.

In this paper, we identify common features of concentration–discharge relationships across a range of hydrochemically distinct catchments with minimal human impacts, and discuss the implications of those features. We then compare several simple models against the

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† The contribution of David W. Clow to this article was prepared as part of his official duties as a United States Federal Government employee.

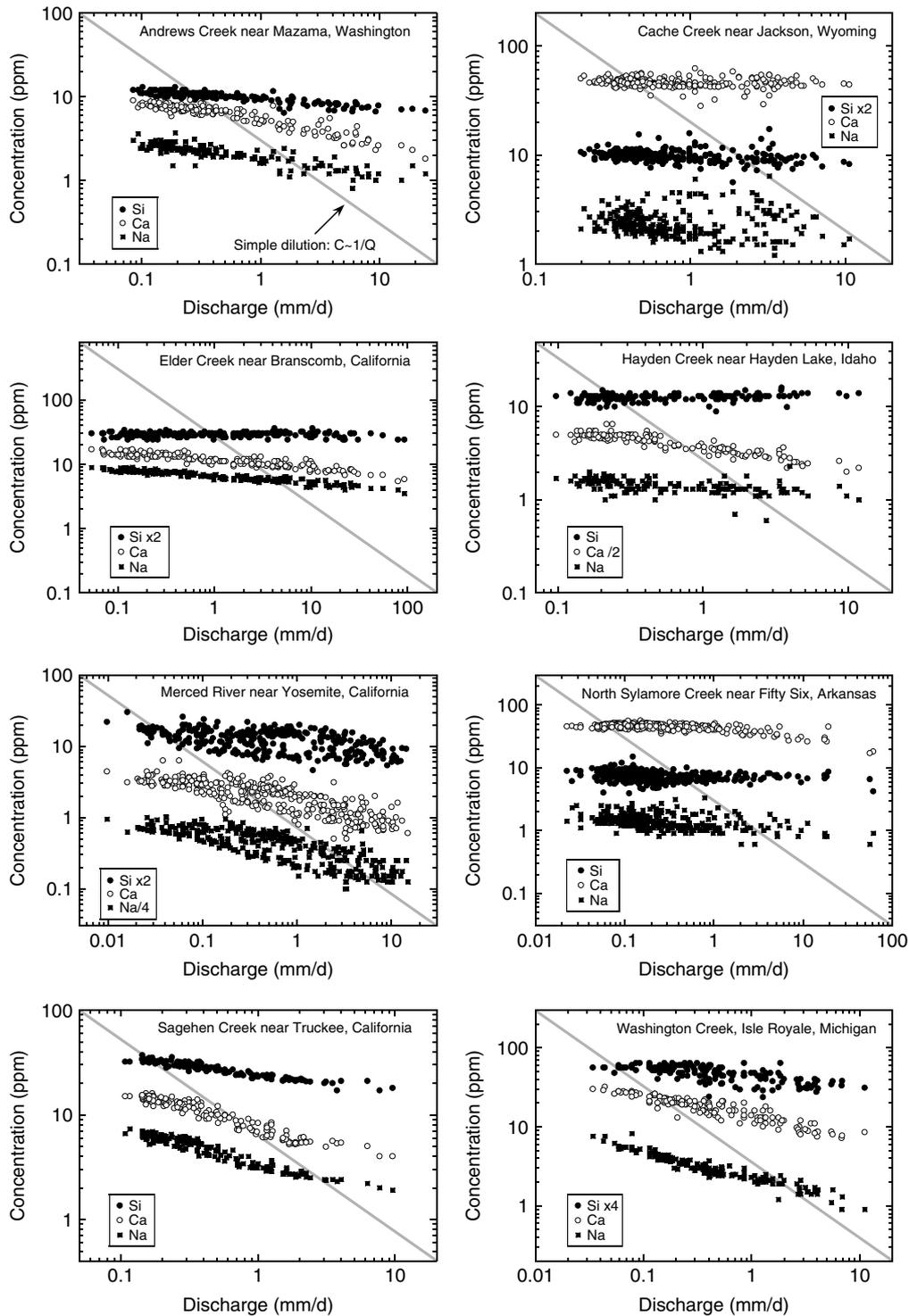


Figure 1. Concentration–discharge relationships for Si, Ca and Na at eight Hydrologic Benchmark Network streams. Each plot has consistent axes (same number of log units for both concentration and discharge), so concentrations determined by dilution of fixed weathering fluxes would have the same slope as the grey diagonal lines shown (log–log slope of -1). Instead, concentration–discharge relationships conform more closely to chemostatic behaviour (log–log slope near zero).

observed patterns in concentration–discharge relationships and evaluate whether their assumptions are generally valid across the study sites. Finally, we show that the concentration–discharge relationships observed in many catchments imply that changes in stream solute fluxes as a result of climatic forcing are, to first order, dependent upon changes in hydrology.

OBSERVATIONS

We plotted concentrations of the major weathering-derived cations (Mg, Na and Ca) and dissolved silica (Si) against instantaneous discharge on logarithmic axes for 59 sites in the United States Geological Survey’s (USGS) Hydrologic Benchmark Network (HBN) (e.g.

Figure 1, discussed further below). The HBN was established in the mid-1960s to provide a long-term database to track changes in the flow and water quality of undisturbed streams and rivers, and to serve as a reference, or 'benchmark', for discerning natural from human-induced changes in river ecosystems (Leopold, 1962). Most HBN sites have more than 30 years of hydrochemical data, and water samples were typically collected five to seven times per year using standard USGS methods (Wilde *et al.*, 1998). The HBN is the only nationwide network of environmental monitoring sites that tracks the health of rivers draining mid-sized, undisturbed basins in the United States. The sites are located throughout the country, usually in National Parks, National Forests or reserves where minimal human influence is expected. Site characteristics compiled from USGS circulars (Mast and Turk, 1999a,b; Clark *et al.*, 2000; Mast and Clow, 2000) are summarized in Table I. Drainage areas range from 6.1 to 5196 km² (median = 146 km²) and average annual runoff varies from 0.7 to 400 cm/year (median = 40 cm/year). Many environments in the United States are represented, including tropical forests, tundra and eight sites with <10-cm average annual runoff, which include arid and semi-arid grasslands, shrublands and semi-desert areas. Most catchments are forested, but several of the basins have substantial alpine and grassland areas. The 59 sites encompass a wide range of lithologic settings (Table I). Solute concentrations in precipitation are not available at all sites for the entire period of record, so the reported concentrations are not corrected by the precipitation chemistry. Stream concentrations of Ca, Na and Mg are at least 10 to 100 times higher than available mean precipitation concentrations. Si concentrations in rainfall are not typically measured, but are normally orders of magnitude lower than Si concentrations in streamflow.

We plotted the concentrations of each of the major weathering-derived solutes against instantaneous discharge. We then calculated simple linear regression statistics for each of the sites and solutes, and, using Student's *t* test, determined whether the best-fit slope was significantly different from reference slopes of zero and -1 (whose meaning is discussed in detail below). We identified sites with non-linear relationships between log concentration and log discharge by examining the residuals of the linear fit. Most of the catchments in the HBN exhibit much less variability in concentrations than in discharge (Figure 1). Figure 1 shows concentration as a function of discharge on logarithmic axes, with the same number of log units shown on each axis to facilitate a visual comparison of the relative variability of concentration and discharge. For example, between high flow and low flow, concentrations at Elder Creek increase by factors of 3 (Ca and Mg), 2.6 (Na) and 1.5 (Si), as discharge changes by a factor of ~ 6000 . Although not plotted in Figure 1, similar relationships also hold for Mg across the HBN sites.

As seen in Figure 1, concentration–discharge plots are often linear on logarithmic axes, indicating that there is a power–law relationship between concentration, C , and

discharge, Q (i.e. $C = aQ^b$, where a and b are constants). The exponent in this power–law relationship (or equivalently, the slope of the concentration–discharge relationship on logarithmic axes) has a physical interpretation. A slope of zero would indicate that the catchment behaves chemostatically, that is, the system keeps concentrations constant as discharge varies. A slope of -1 , on the other hand, would indicate that concentrations vary inversely with discharge, as might be expected if dilution were the dominant process controlling concentrations, such that approximately constant fluxes of solutes were diluted by variable fluxes of water.

Power-law concentration–discharge relationships like those shown in Figure 1 can be usefully summarized by their log–log slopes. The best-fit $\log(C)$ – $\log(Q)$ slopes for each solute can then be compared across all 59 of the HBN sites (Figure 2) and can be compared to reference slopes of zero (chemostatic behaviour) and -1 (dilution). Uncertainty in the best-fit slope of ± 1 standard error (SE) is indicated by error bars, which are shown if they are larger than the plotting symbols. Across all sites, slopes are generally slightly less than zero. The means of the best-fit log–log concentration–discharge slopes vary between approximately -0.05 and -0.15 (SE of the slope ~ 0.01 – 0.02) for each of the solutes. No slope is within two SEs of -1 and only four (Na), six (Mg), eight (Ca) and 14 (Si) of the 59 sites have slopes within two SEs of zero. Slopes across all sites and solutes are strikingly similar. In general, Si slopes are closer to zero than the slopes of the other solutes. With few exceptions (discussed below), nearly all of the concentration–discharge relationships in this study can be described by power–law relationships with small negative exponents. The data in Figure 2 show that most catchments behave almost chemostatically for chemical weathering products such as Ca, Mg, Na and Si.

Although this near-chemostatic behaviour is common, examination of residual plots for all sites and solutes reveals that the best fits for up to 10% of the sites may not be power-law. Such sites are marked by open circles in Figure 2 and the plotted slope of the linear fit only provides a general sense of the concentration–discharge relationship for these sites. We also calculated the ratio of the standard deviation of log discharge to log concentration for all sites and solutes (not shown) to quantify the relative variability of discharge and concentration without making any assumptions about the form of the concentration–discharge relationship. Only Upper Three Runs, SC had Ca and Mg concentrations that were more variable than its discharge, and only Castle Creek, SD and Dismal River, NE had more variable Na concentrations. No sites had Si concentrations that were more variable than discharge. The ratio of the standard deviations of log discharge to log concentration ranged from just below 1 to 21.5, with the median ratio equal to 4.1 (Ca), 4.0 (Mg and Na), and 5.3 (Si). These observations reinforce the inference drawn from the shallow power-law slopes, namely that these catchments behave almost

Table I. Site characteristics for the 59 Hydrologic Benchmark Network sites discussed in this analysis, as compiled from USGS Circulars 1173 A–D, unless otherwise indicated by one of the footnotes detailed at the bottom of this table

Station name	Station number	Drainage area [km ²]	Average annual runoff [cm]	Land cover/use	Lithology	Low mean monthly temperature [°C]	High mean monthly temperature [°C]	Mean annual precipitation [cm]
Andrews Creek near Mazama, WA	12 447 390	57	48	Subalpine forest	Quartz monzonite, quartz diorite	4	10	89 ^a
Bear Den Creek near Mandaree, ND	06 332 515	192	3	Grassland, agriculture	Sandstone, siltstone, alluvium, colluvium	-12.3	20.5	39
Beauvais Creek near St. Xavier, MT	06 288 200	259	9	Prairie	Slate, shale, sandstone	-11.1 ^a	31.5 ^c	38 ^a
Beaver Creek near Finley, ND	05 064 900	415	2	Prairie, agriculture, grazing	Glacial till	-14.8	21	49
Big Creek at Pollock, LA	07 373 000	132	44	Pine forest, agriculture, residential	Unconsolidated alluvium	8.2	27.8	148
Big Jacks Creek near Bruneau, ID	13 169 500	655	0.7	Sagebrush	Rhyolite/basalt	-0.5	22.9	19.6
Biscuit Bk above Pigeon Bk at Frost Valley, NY	01 434 025	10	91	Mixed forest, residential	Shales, sandstones, conglomerates	5 ^b	N/A	157 ^b
Blackwater River near Bradley, AL	02 369 800	227	59	Pine forest hills, bay wetland	Sandstone	9.1	26.2	150
Blue Beaver Creek near Cache, OK	07 311 200	64	19	Grassland/prairie	Rhyolite, conglomerates, sandstone	3	27.8	77
Buffalo River near Flat Woods, TN	03 604 000	1158	59	Deciduous forest, agriculture, residential	Limestones, siltstone, shale	3.3	25	127
Cache Creek near Jackson, WY	13 018 300	27	40	Pine/fir, grassland	Limestone, dolomite, siltstone, sandstone, shale	-9.2	16	61 ^a
Castle Ck above Deerfield Res. near Hill City, SD	06 409 000	205	5	Pine forest	Schist, limestone	-7.3	15.5	51
Cataloochee Creek near Cataloochee, NC	03 460 000	127	78	Broadleaf forest	Sandstone	0	16	145
Cossatot River near Vandervoort, AR	07 340 300	232	78	Pine-oak forest, residential	Metamorphosed sedimentary: chert, sandstone, shale, novaculite	5	27.2	130
Cypress Creek near Janice, MS	02 479 155	136	70	Pine forest	Fine-grained sedimentary, quartz, salt dome	9.1	27.4	152
Dismal River near Thedford, NE	06 775 900	2500	7	Prairie, grazing	Chalk, limestone, shale, unconsolidated sediments	-5.4	23.7	54
Elder Creek near Branscomb, CA	11 475 560	16.8	129	Mixed forest, chaparral, grassland	Sandstone, argillite	6	31	215

Table I. (Continued)

Station name	Station number	Drainage area [km ²]	Average annual runoff [cm]	Land cover/use	Lithology	Low mean monthly temperature [°C]	High mean monthly temperature [°C]	Mean annual precipitation [cm]
Elk Creek near Decatur City, IA	06 897 950	136	23	Prairie, deciduous trees, agriculture	Limestone, shale, alluvium, loess	-6.6	24.6	92
Encampment River above Hog Park Creek near Encampment, WY	06 623 800	188	50	Montane/subalpine forest, grassland	Granite, quartz monzonite, granodiorite, felsic gneiss, calcareous siltstone, shale, mudstone, till	-5.8	17.2	76
Esopus Ck at Shandaken, NY	01 362 198	165	74	Mixed forest, residential	Shale, sandstone, conglomerate	-4.2	21.5	157
Falling Creek near Juliette, GA	02 212 600	187	30	Mixed forest	Gneiss, gabbro	7.3	26.6	122
Halfmoon Creek near Malta, CO	07 083 000	61	40	Coniferous forest, tundra	Biotite gneiss, schist, migmatite	-8.9	12.2	53 ^a
Hayden Creek below N Fork near Hayden Lake, ID	12 416 000	57	44	Coniferous forest	Quartzite, argillite, siltstone, dolomite, limestone	-2	21	89
Holiday Creek near Andersonville, VA	02 038 850	22	35	Mixed forest	Phyllite, schist, gneiss	3	25	105
Honolii Stream near Papaikou, HI	16 717 000	31	377	Lava, tropical vegetation	Basalt	17.6 ^c	28.8 ^c	328 ^{c,k}
Kahakuloa Stream near Honokohau, Maui, HI	16 618 000	8	197	Dense tropical vegetation	Basalt	17.4 ^d	31.1 ^d	N/A
Kawishiwi River near Ely, MN	05 124 480	655	28	Mixed forest	Anorthosite, igneous intrusives, till	-14.4	19.2	70
Kiamichi River near Big Cedar, OK	07 335 700	104	74	Mixed forest	Shale, siltstone, sandstone	4.9	27.2	130
Kings Creek near Manhattan, KS	06 879 650	10.6	20	Tallgrass prairie	Shale, limestone	-1.8	26.6	84
Limpia Creek above Ft. Davis, TX	08 431 700	135	1.6	Deciduous forest, desert and riparian plants	Andesite, basalt	7.1 ^e	25 ^e	45 ^e
Little River above Townsend, TN	03 497 300	275	93	Broadleaf forest	Phyllite, sandstone, slate, limestone	4	23	152 ^{i,j}
McDonalds Branch in Lebanon State Forest, NJ	01 466 500	6.1	32	Broadleaf forest/swamp	Unconsolidated sediments	12.8	25 ^f	116
Merced River at Happy Isl. Bridge near Yosemite, CA	11 264 500	469	66.5	Mixed forest, meadow	Granite, granodiorite	3	22	94

Table I. (Continued)

Station name	Station number	Drainage area [km ²]	Average annual runoff [cm]	Land cover/use	Lithology	Low mean monthly temperature [°C]	High mean monthly temperature [°C]	Mean annual precipitation [cm]
Minam River at Minam, OR	13 331 500	622	65	Coniferous forest, grasslands, meadow	Granite, intruded by aplite, pegmatite, basalt	-7.2	14.6	100 ^{h,i}
Mogollon Creek near Cliff, NM	09 430 600	179	17	Mixed forest, meadow	Rhyolite, quartz latite, porphyritic flows, plagioclase, brotite, sanidine	3.6	24.4	37
North Fork Quinault R near Amanda Park, WA	12 039 300	192	402	Conifers, alpine vegetation, bare rock	Basalt, semi-consolidated sediments, slate	1.4 ^c	25.4 ^c	328 ^{c,i}
North Fork Whitewater River near Elba, MN	05 376 000	262	17	Agriculture, broadleaf forest	Limestone, dolomite, shale, sandstone, till	-10.7	22.7	84
North Sylamore Creek near Fifty Six, AR	07 060 710	150	28	Hardwood/pine forest	Sandstone, dolomite, shale, limestone	1.9	26.2	112
Popple River near Fence, WI	04 063 700	360	29	Mixed forest	Granite and granitoid gneiss	-17.1	20.9	78
Red Butte Ck at Ft. Douglas near Salt Lake City, UT	10 172 200	18.8	20	Mixed forest, grassland	Quartzite, sandstone, limestone	-0.7	25.4	74 ^a
Rio Mora near Terrero, NM	08 377 900	138	20	Coniferous forest, meadow	Granite, amphibolite, tonalite, quartz diorite, quartzite, schist, limestone	-2.2	15.8	45
Rock Ck below Horse Ck near Intl Boundary, MT	06 169 500	850	1.5	Prairie, agriculture, grazing	Shale, unconsolidated sediments	-13.5	18.8	29
Sagehen Creek near Truckee, CA	10 343 500	27	40	Coniferous forest, meadow	Granite, andesite, breccia, hornfels, till, alluvium	-3	17	94
Scape Ore Swamp near Bishopville, SC	02 135 300	249	38	Mixed forest, agriculture	Arkosic and argillaceous sands	5.5	25.5	115
Sipsy Fork near Grayson, AL	02 450 250	239	62	Mixed forest	Limestone, sandstone, shale, mudstone, claystone, nonpersistent coal beds	5	25.5	145
Sopchoppy River near Sopchoppy, FL	02 327 100	265	67	Mixed forest	Limestone, unconsolidated marine sediment	12.2	27.4	145
South Fork Rocky Creek near Briggs, TX	08 103 900	86	11	Arid grassland	Limestone, marl, dolomite	8.4	28.2	75
South Hogan Creek near Dillsboro, IN	03 276 700	99	39	Broadleaf forest, agriculture, grazing	Limestone, shale, glacial till, loess	-1.9	22.9	100

Table I. (Continued)

Station name	Station number	Drainage area [km ²]	Average annual runoff [cm]	Land cover/use	Lithology	Low mean monthly temperature [°C]	High mean monthly temperature [°C]	Mean annual precipitation [cm]
South Twin River near Round Mountain, NV	10 249 300	52	11.4	Forest, sagebrush, semi-desert	Felsite, tuff, quartzite, limestone, dolostone, quartz	-1.4	22.2	20 ^{h,i}
Steploe Creek near Ely, NV	10 244 950	29	22	Forest, scrub, semi-desert	Limestone, shale	-4.3	19.6	24 ^{h,i}
Talkeetna River near Talkeetna, AK	15 292 700	5196	70	Mixed forest, mixed shrubs, tundra	Glacial drift, colluvium, igneous bedrock	-11.7 ^g	14.9 ^g	72 ^g
Tallulah River near Clayton, GA	02 178 400	146	116	Broadleaf forest	Gneiss, schist, amphibolite	3.3	21.6	182
Upper Three Runs near New Ellenton, SC	02 197 300	255	36	Mixed forest	Arkosic sands	7.5	27.1	120
Upper Twin Creek at McGaw, OH	03 237 280	31.6	38	Broadleaf forest	Sandstone, shale	0	24.4	105
Vallecito Creek near Bayfield, CO	09 352 900	187	70	Coniferous forest, alpine tundra	Slate, schist, quartzite, breccia, limestone, conglomerate, quartz monzonite, granite	-5.9	17.6	117 ^a
Washington Creek at Windigo Isle Royale, MI	04 001 000	34	42	Mixed forest	Basalt, andesite, sandstone, glacial drift	3.4 ^e	N/A	77
Wet Bottom Creek near Childs, AZ	09 508 300	94	15.5	Semidesert, grassland, woodlands	Granite, basalt, andesite, siltstone, dolomite, limestone	7.7	29.4	63.5
Wild River at Gilead, ME	01 054 200	180	89	Mixed forest	Sandstone, shale, siltstone, gneiss, mica schists, quartzites	-9	19	119
Young Womans Creek near Renovo, PA	01 545 600	120	56	Mixed forest	Sandstone, siltstone, shale, conglomerate, discontinuous coal beds	-3.3	22.5	105

^a Hydroclimatic Data Network (HCND).

^b Murdoch and Stoddard (1992).

^c Desert Research Institute (DRI).

^d National Weather Service of the National Oceanic and Atmospheric Administration (NWS/NOAA).

^e Mean annual temperature (not low or high) and therefore not used in empirical model.

^f Data from Silas Little Experimental Forest.

^g National Climatic Data Centre (NCDC/NOAA).

^h Low elevation estimate.

ⁱ Varies strongly with elevation.

^j North Carolina State University (NCSU/NOAA).

^k Mean annual precipitation in Hilo, HI.

^l Mean annual precipitation in Amanda Park, WA.

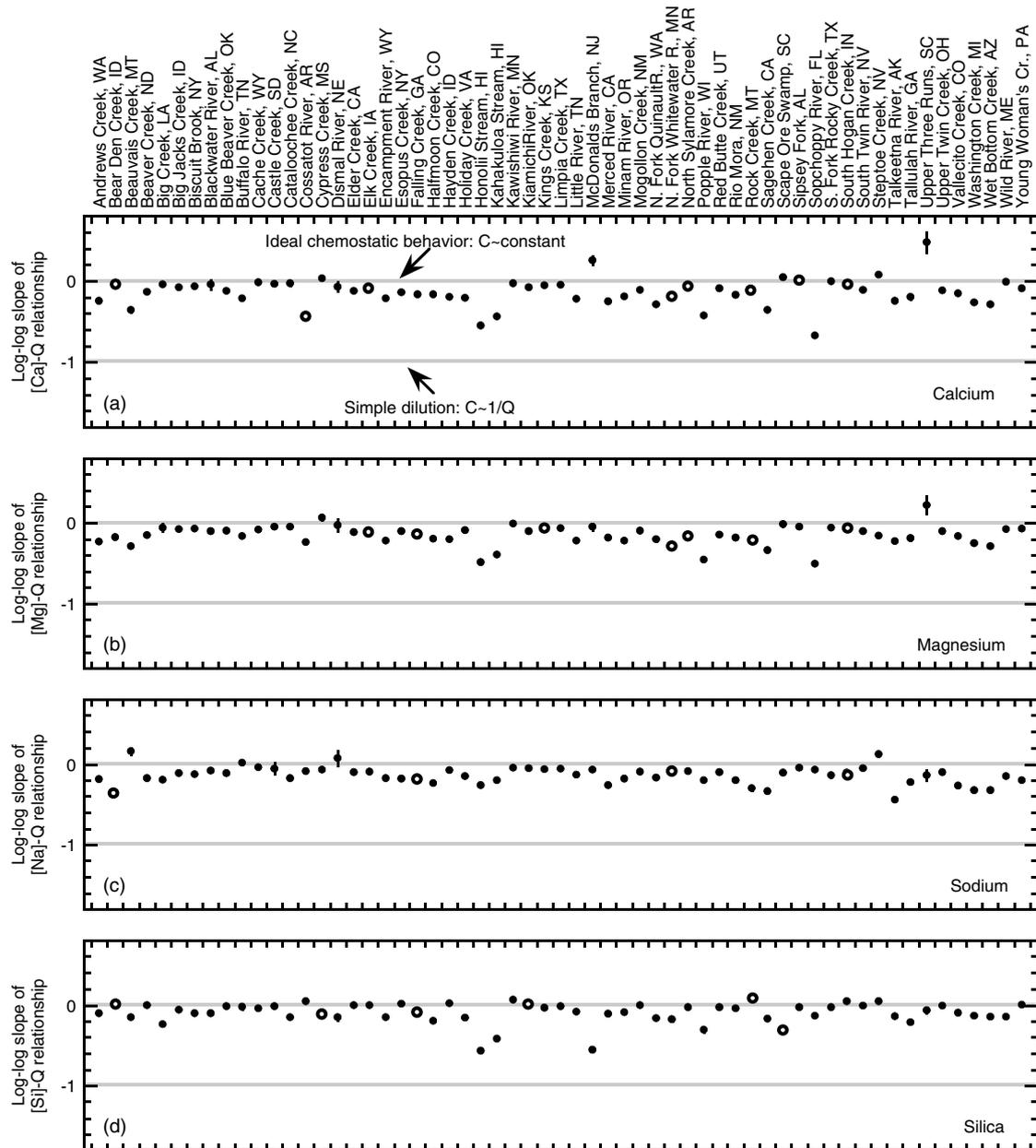


Figure 2. Log–log slopes of concentration–discharge relationships for 59 Hydrologic Benchmark Network streams arranged alphabetically by site name. Grey lines indicate slope values expected for ideal chemostatic behaviour (concentration held constant; log – log slope = 0) and for simple dilution of a constant solute flux (concentration inversely proportional to discharge; log – log slope = –1). With few exceptions, these catchments exhibit nearly ideal chemostatic behaviour for Ca, Mg, Na and Si. Error bars indicate ± 1 standard error, and are shown where they are larger than the plotting symbols. Open symbols indicate that the observed relationship appears to be non-linear in log–log space.

chemostatically. We also verified that the samples collected are representative of the range of flows at each site. At all sites, samples are collected across a range of flows from the 5th to 97th flow percentiles (as calculated from the complete flow record reported in the USGS National Water Information System database, excluding dates on which flow is zero). Most sites include samples from the 1st to 99th percentiles of flow, and median HBN samples corresponded approximately to the 52nd flow percentile, suggesting that base flows are not oversampled.

A handful of sites have positive slopes for one or more solutes, which indicate that concentration increases with increasing flow (e.g. Upper Three Runs, SC for Ca

and Mg and Steptoe Creek, NV for Na). In past studies, increased concentrations of more biologically active ions such as K^+ and NO_3^- with increased flow have been attributed to leaching from organic soil horizons during higher flows (Walling and Webb, 1986). At the HBN sites, the observed increase in concentration of the major weathering products with discharge may be due to a weak correlation between discharge and concentration, or due to limited variability in the sampled discharge (e.g. discharge varies by only a factor of ~ 4 at Upper Three Runs). At Upper Three Runs, it also may be a result of analytical error or instrumentation changes in very dilute stream waters (Mast and Turk, 1999a, pp.

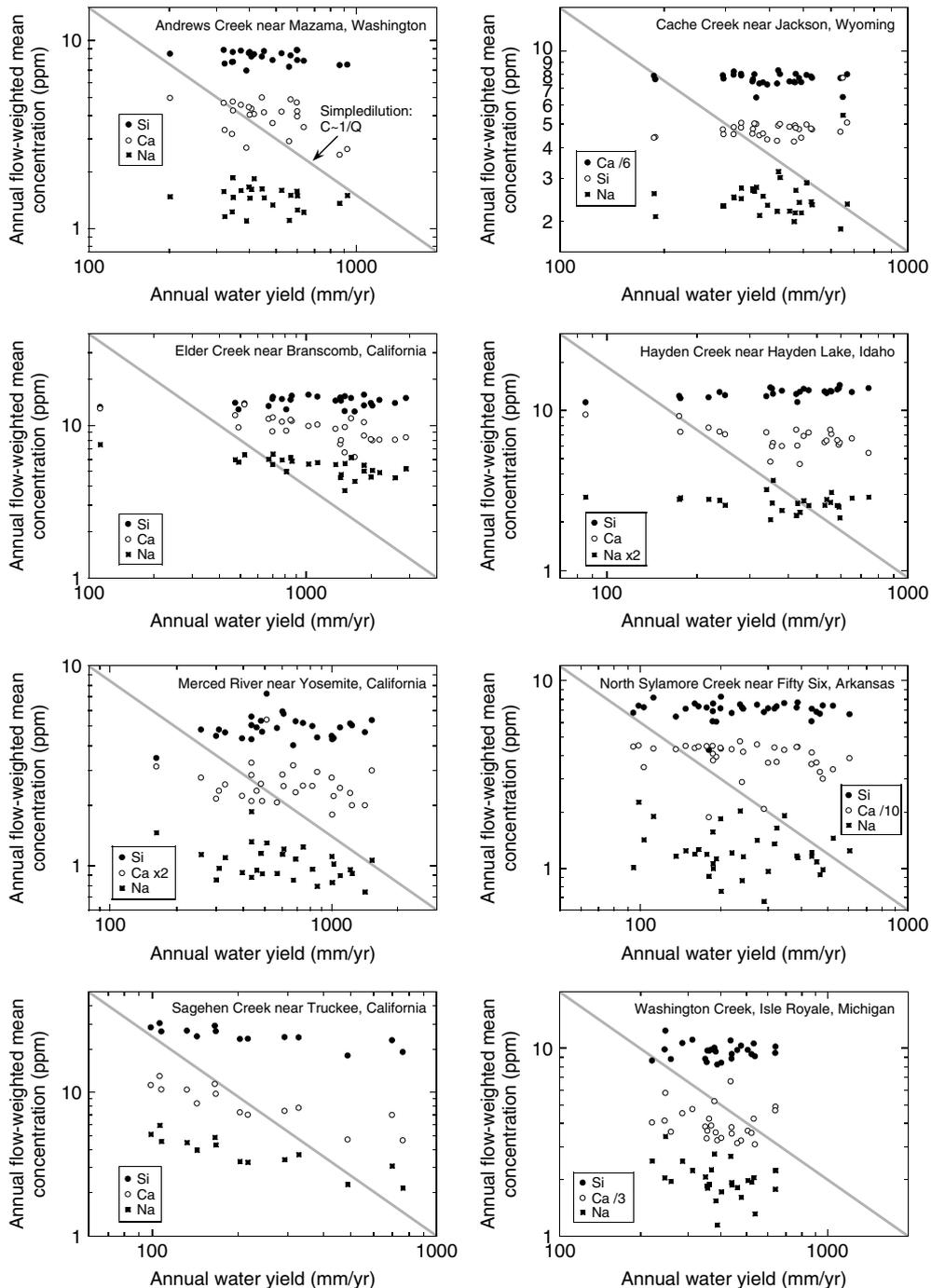


Figure 3. Annually averaged concentration–discharge relationships for Si, Ca and Na at the same eight Hydrologic Benchmark Network streams shown in Figure 1. Each plot has consistent axes (same number of log units for both concentration and discharge), so concentrations determined by dilution of fixed weathering fluxes would have the same slope as the grey diagonal lines shown (log–log slope of -1). Even on inter-annual time scales, concentration–discharge relationships do not generally follow the predictions of a simple dilution model, instead conforming more closely to chemostatic behaviour (log–log slope near zero).

108–110). However, most sites show little variability in concentration with discharge and we focus on these sites for the rest of this paper.

One might postulate that concentrations are relatively constant across wide ranges of discharge simply because the volume of water stored in a catchment is much larger than the amount discharged during an individual storm event. Therefore we also tested whether catchments behave chemostatically on inter-annual time

scales. Annualized concentration–discharge relations for each of the HBN sites were plotted as mean annual flow-weighted concentrations against annual water yield. Water yield was calculated by summing all daily flows in the water year, as available from the daily USGS streamflow record, and dividing by catchment area. Mean flow-weighted concentrations were calculated as $\Sigma(Q_i C_i) / \Sigma Q_i$, where the subscript i indicates each sample during the water year. We excluded years with fewer

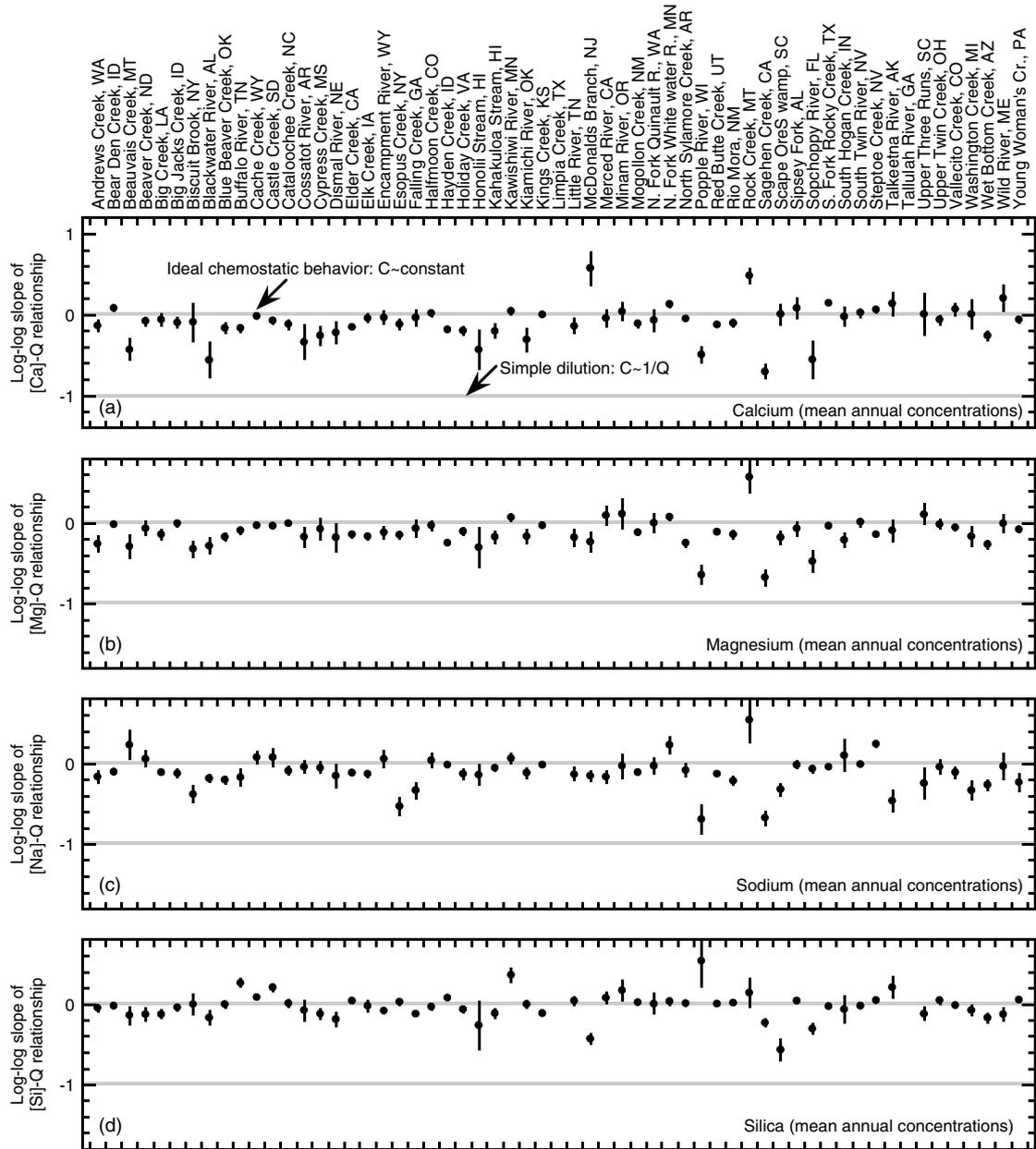


Figure 4. Log–log slopes of relationships between mean annual flow-weighted concentrations and mean annual discharge for 57 Hydrologic Benchmark Network streams (slopes are not shown for Limpia Creek, TX or Tallulah River, GA because too few years of data are available). Grey lines indicate slope values expected for ideal chemostatic behaviour (concentration held constant; log – log slope = 0) and for simple dilution of a constant solute flux (concentration inversely proportional to discharge; log – log slope = –1). Even on inter-annual time scales, almost all of these catchments exhibit nearly ideal chemostatic behaviour for Ca, Mg, Na and Si. Error bars indicate ± 1 standard error calculated from a weighted least squares fit to the log annual flow-weighted concentration for each water year versus log annual water yield. The weighting function is equal to the inverse unbiased weighted variance of the log concentration. By unbiased, we mean that we account for a potential loss in the degrees of freedom introduced by variable flow by calculating the effective number of solute measurements per water year.

than four available concentration measurements from the inter-annual concentration–discharge analysis.

The plots of mean annual flow-weighted concentrations versus annual water yield exhibit similar patterns to those observed on an event basis (Figures 3 and 4). Mean annual concentrations vary much less than water yield does from year to year. The concentration–discharge plots for inter-annual time scales (Figure 3) are similar to those for individual samples (Figure 1); both exhibit power-law relationships between solute concentrations and water yields, with small negative log–log slopes.

Across the HBN sites, these log–log slopes are generally close to zero on both inter-annual time scales (Figure 4) and event time scales (Figure 2), although the error bars in Figure 4 are larger because the annualized concentration–discharge plots (e.g. Figure 3) have fewer points and a smaller range of discharge. The near-zero slopes imply that catchments exhibit near-chemostatic behaviour over both event and inter-annual timescales and across a wide range of hydrologically and geochemically diverse sites. Thus, an interesting first-order question is not why concentrations of weathering products

vary, but why they vary so little as discharge changes so much.

ASSESSMENT OF ALTERNATIVE MODELS

Consistent near-zero $\log(C)$ - $\log(Q)$ slopes imply that rates of solute production or mobilization must be nearly proportional to water fluxes on intra- and inter-annual timescales. Here we explore several simple quantitative explanations for the observed concentration–discharge patterns to verify if they hold across all the HBN sites, and to compare different possible models at each site. We evaluate these explanations on the basis of several key criteria. They should generate power–law relationships between concentration and discharge with small negative slopes and little hysteresis. Furthermore, they should have reasonable physical and chemical parameters and should make plausible assumptions about catchment behaviour. They should be as simple as possible and explain observations in a wide range of catchments. We examine several empirical, mixing and chemical models to gain insight into the linkages between chemical weathering and hydrologic processes that produce the observed concentration–discharge relationships. We quantitatively assess the models' performance at each site using the Akaike and Bayesian information criteria (AIC and BIC) for each set of comparable models.

Empirical models

We first evaluated whether the slope of the concentration–discharge relationship can be predicted as a simple empirical function of each catchment's characteristics, or as a multivariate model of several characteristics. For each site, we plotted average low and high temperature, annual average runoff, area, and Mean Annual Precipitation (MAP) against the event-based concentration–discharge slope for each solute, and calculated the correlation between each of these site characteristics and each solute's concentration–discharge slope (using the non-parametric Spearman correlation coefficient because the distributions of site characteristics are not normal). Based on the site descriptions from the USGS circulars (Mast and Turk, 1999a,b; Clark *et al.*, 2000; Mast and Clow, 2000), we also coded each site according to the presence or absence of carbonates and volcanics in the underlying bedrock. We then used the F-test (Zar, 1984) to determine whether the presence of either of these broad rock types significantly affected the concentration–discharge slope for any solute. For the multivariate models, we systematically added and removed characteristics from a series of multiple linear regression models and evaluated their performance.

The site characteristics that we tested generally do not satisfactorily explain the observed slopes of the concentration–discharge relationships (Table II). Steeper concentration–discharge slopes are associated with higher average annual runoff (although, surprisingly, not

always with higher MAP); these correlations are statistically significant for some solutes but not others. Sites with volcanic bedrock have significantly ($p < 0.05$) steeper concentration–discharge slopes for Ca, Mg and Na compared to sites where volcanics are absent. Similarly, log–log slopes for Na are significantly ($p < 0.02$) shallower at sites with carbonate bedrock, compared to sites without carbonates. Although some site characteristics show statistically significant effects on concentration–discharge slopes, their predictive power is weak because they explain only a small fraction of the variance; typical r^2 values are 0.1 or less. Multivariate models with combinations of these site characteristics could only explain <20% of the variability in $\log(C)$ - $\log(Q)$ slopes. We conclude that the observed variation in concentration–discharge slopes cannot be straightforwardly predicted by any of the site characteristics tested here. Other site characteristics, such as basin slope, soil permeability, or amount and type of soil and vegetation, might be useful explanatory variables, but they have not been quantified for most of the HBN basins. Basin slope and soil permeability, for example, might be important because they influence hydrological flow paths and the residence time of water in the basins.

Mixing models

We turn from empirical models based on site characteristics to simple models based on the mixing of waters with different compositions. Isotopic studies and other hydrometric and hydrochemical evidence have shown that in many catchments, typical residence times are much longer than the duration of individual storm events

Table II. Statistical tests of association between site characteristics and concentration–discharge slopes across the 59 HBN streams

F ratio	Ca	Mg	Na	Si
Volcanics (present vs. absent)	5.32 ^a	6.51 ^a	4.59 ^a	3.77
Carbonates (present vs. absent)	0.07	0.02	12.47 ^b	2.54
Spearman correlation coefficient, r_s	Ca	Mg	Na	Si
Average annual runoff (cm)	-0.27 ^a	-0.19	-0.21	-0.28 ^a
Average low temperature (deg C)	-0.02	0.10	0.06	-0.30 ^a
Average high temperature (deg C)	-0.06	0.06	0.25	-0.16
MAP, Mean annual precipitation (cm)	0.03	0.05	-0.08	-0.28 ^a
Area (km ²)	-0.11	-0.08	0.00	0.04

Superscripts a and b indicate statistical significance at the $p < 0.05$ and $p < 0.02$ levels, respectively. Several of the tested relationships are statistically significant but their explanatory power is low. Sites with volcanic bedrock have steeper concentration–discharge slopes for Ca, Mg and Na than sites without volcanics, and slopes for Na are shallower at sites with carbonate bedrock compared to sites without carbonates. Nonparametric (Wilcoxon) tests agree with the parametric (F-test) results. Average annual runoff is significantly correlated with Ca and Si slopes, and average low temperature and MAP with Si slopes, according to the robust Spearman rank correlation coefficient.

(e.g. Buttle, 1994). One can imagine that residence times may be long enough for weathering reactions to approach equilibrium, and that this explains the chemostatic behaviour observed across the HBN sites. Sufficient storage capacity for the ‘old’ water must exist for this option to be physically plausible, and we explore storage requirements for different models below. In general, we find that mixing models that assume a constant rate of solute supply generally cannot reproduce the observations well.

First, we present a simple ‘bucket’ mixing model that treats the catchment as a single well-mixed reservoir whose volume (V , [m³]) remains constant as discharge (Q_w , [m³/s]) varies. The model likewise assumes that the solute flux (Q_s , [ppm–m³/s]) produced by mineral weathering is constant through time. It further assumes that concentrations in precipitation are very dilute compared to streamflow (as is typically the case for the major weathering products), so that precipitation solute fluxes can be ignored in the mass balance. Under these conditions, the solute concentration (C , [ppm]) in the well-mixed reservoir, and thus in its outflow, will evolve according to the familiar mass-balance equation:

$$\frac{dC}{dt} = \frac{(Q_s - Q_w C)}{V} \quad (1)$$

where Q_w is the average daily water flux through the reservoir, for which we use the USGS historical daily flow record. We fix the solute flux (Q_s) equal to the product of the average water flux and the flow-weighted average concentration, so that the average modeled solute flux will equal the observed long-term average. The reservoir volume (V) is the only free parameter, which is adjusted to reproduce the observed range of variation in outflow concentrations.

Constraining the concentrations modeled using Equation (1) within the bounds of observed variability in the HBN data set requires a storage volume that is well-mixed to depths of several meters throughout the

Table III. Subsurface storage depths required for a simple ‘bucket’ model assuming a constant 5%, 10% and 30% porosity for the model described in Equation (1) of the text

Site	Storage Depth (m)		
	5% porosity	10% porosity	30% porosity
Andrews	10.8	5.4	1.8
Cache	10.1	5.0	1.7
Elder	83.7	41.9	14.0
Hayden	6.0	3.0	1.0
Merced	9.8	4.9	1.6
N Sylamore	6.5	3.3	1.1
Sagehen	21.7	10.9	3.6
Washington	9.2	4.6	1.5

The porosity is a single average value for all soil and underlying bedrock to the specified depth. The specified storage depth indicates the volume required to maintain the observed variability in concentrations at a given site (reported value is the median storage for all four solutes based on the observed ratio of maximum to minimum concentrations at each site, the median of which is ~ 4 across all sites and solutes).

catchment (Table III) for a porosity of 10% (averaged across both soil and underlying rock). Higher porosities require a smaller storage volume whereas lower porosities require a larger storage volume. Even with sufficiently large storage volumes, however, modeled concentration–discharge relationships do not match the observations well; the model results exhibit large hysteresis loops that are not present in the observations (Figure 5a). These loops result from the assumption that the catchment behaves as a simple well-mixed bucket: the integro-differential relationship in Equation (1) implies a 90-degree phase lag between changes in discharge and changes in concentration, rather than the simultaneous variations in concentration and discharge that are usually observed. Hysteresis loops are frequently observed in concentration–discharge relationships, but the extent of looping modeled in Figure 5a is much greater than is typically observed (e.g. Evans and Davies, 1998). To match the observed concentration–discharge relationships, this model would have to be modified to allow solutes to be: (1) produced at a variable rate or (2) mobilized from different sources at variable rates.

Another well-known model that we consider is the Hubbard Brook ‘working model’ (Johnson *et al.*, 1969) which assumes that discharge is proportional to storage volume (V , [m³]), and that solute concentrations (C , [ppm]) associated with each storage volume are fixed. Storage volume is defined as the subsurface pore space available above an ‘impermeable’ layer. C is then inversely related to Q according to:

$$C = \left[\frac{d}{(1 + bQ)} \right] + a \quad (2)$$

where a = concentration of solute in the low-concentration end-member [ppm], b = mean residence time/ $V_{Q=0}$ (flows at the catchment outlet are assumed to cease at some non-zero storage volume, $V_{Q=0}$) (s/m³), and d = concentration difference between high and low concentration waters [ppm]. Any non-zero flow is directly proportional to water in storage above the minimum volume. One can immediately see that this model does not represent a power-law relationship between C and Q , but instead that the relationship is a hyperbolic function. However, because it has an additional free parameter, Equation (2) can also fit the data well (Figure 5b). A non-linear fitting algorithm which minimizes the sum of squared error between the model results and observed data is used to select best-fit values of a , b , and d . The parameter b depends only on the mean residence time of water in the catchment and the minimum volume required for flow in the stream. Importantly, b does not depend on the solute of interest; therefore, it should have the same value for all the solutes at an individual site. This consistency in b can be ensured by simultaneously fitting all solutes in a given catchment. Johnson *et al.* (1969) suggest that a should be thought of as the ‘rainwater’ concentration of each solute. However, the best-fit a values exceed measured volume-weighted precipitation concentrations for Ca, Mg and Na [as reported in Mast and Turk

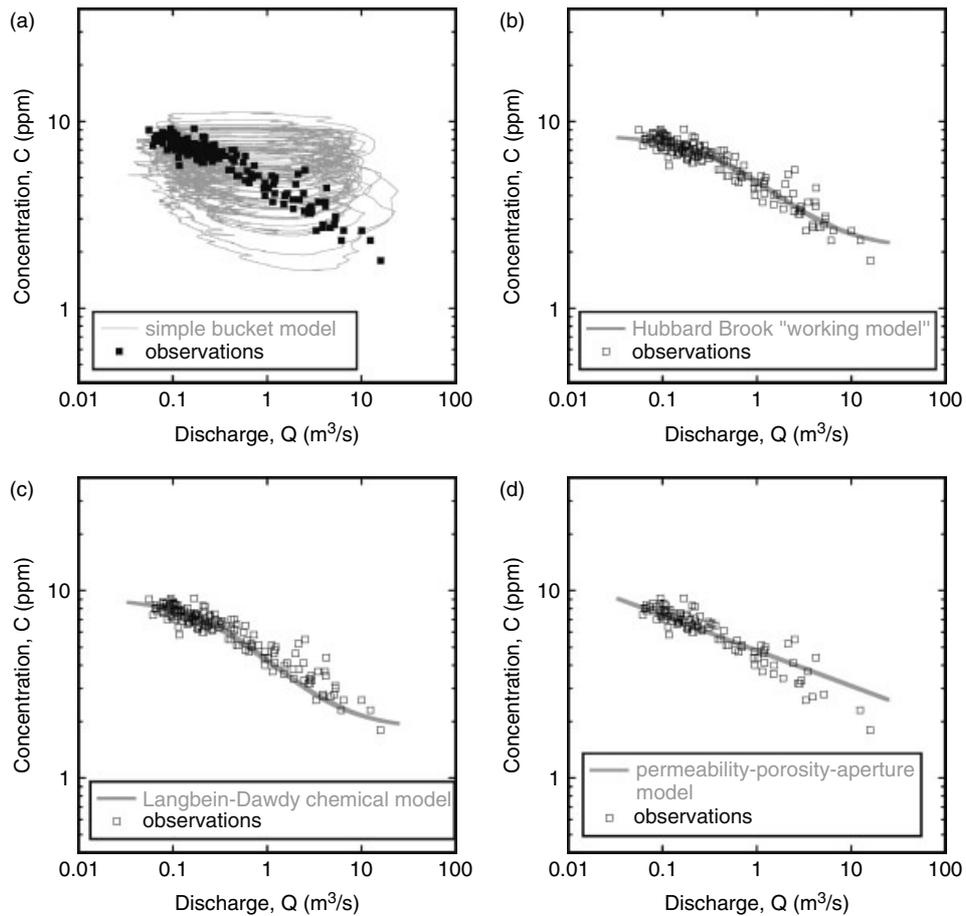


Figure 5. Concentration (C)–discharge (Q) relationships for several models plotted with the observed values for Ca at Andrews Creek in Mazama, WA. (a) A well-mixed reservoir model (Equation (1)) with a very large storage volume can reproduce the observed range in concentration variability, but only with excessively large hysteresis loops that are not observed in the real data. (b) Inverse relationship between C and Q as specified by the Hubbard Brook ‘working model’ (Johnson *et al.*, 1969) generally matches the form for each solute, but best-fit a parameters (Eq. 2) exceed observed rainfall concentrations (Table IV). (c) Langbein and Dawdy’s (1964) chemical mixing model can fit the data well but allows no storage of water or mixing of waters of different ages in the catchment. (d) The permeability-porosity-aperture model (see text) can also fit the data reasonably well, although its assumptions still need to be tested in the field. The slight overestimate of concentration at high discharges is due to the simultaneous fitting to all four solutes with one hydrologic parameter, b_0 , which is the best-fit slope to all four solutes’ concentration–discharge data. See text for more detailed discussion.

(1999a,b); Clark *et al.* (2000); Mast and Clow (2000)] by up to two orders of magnitude (Table IV). Concentrations of Si in precipitation are not generally reported, but the best-fit a for Si is in the range of ~ 10 ppm. Instead of

representing ‘rainfall’ concentrations, the high best-fit a values could perhaps be thought of as ‘soil water’ concentrations. In any case, the fact that the best-fit values of a are much higher than rainfall concentrations implies

Table IV. Best-fit parameter a in the Hubbard Brook ‘working model’ and observed precipitation concentrations for the major base cations at eight representative sites

All (ppm)	Best-fit a_{Ca}	Observed Ca in precipitation	Best-fit a_{Mg}	Observed Mg in precipitation	Best-fit a_{Na}	Observed Na in precipitation
Andrews	2.04	0.03	0.31	0.02	0.97	0.07
Cache	44.1	0.19	12.3	0.02	2.20	0.04
Elder	7.21	0.04	2.34	0.04	4.32	0.18
Hayden	4.23	0.11	1.31	0.04	1.13	0.01
Merced	0.72	0.05	0.10	0.01	0.56	0.04
N Sylamore	28.6	0.14	1.89	0.02	0.82	0.05
Sagehen	3.56	0.05	1.36	0.01	1.75	0.04
Washington	7.99	0.16	2.44	0.03	1.14	0.02

Observed Si concentrations in precipitation were not available. The best-fit concentrations, a , are observed to be one to two orders of magnitude higher than the observed concentrations. This suggests that the model is unable to represent some mixing or reaction processes occurring in the catchment. In all cases, all three parameters in Equation (2) were fit simultaneously for all four solutes; a and d were constrained to be ≥ 0 , and b , which depends only on hydrology and is independent of the solute, was forced to be a single value for all four solutes at each site.

that important solute sources within the catchment are not captured by the model.

Chemical models

On the other end of the modeling spectrum, one could assume that waters react so rapidly with soil and rock that one can ignore mixing of waters of different ages altogether. If changes in chemical reactions were solely responsible for the concentration–discharge patterns we see, what would this imply? The simplest way to maintain chemical concentrations as discharge increases is through a combination of increasing reactive surface area and increasing reaction rates.

A simple approach was proposed by Langbein and Dawdy (1964) who assumed that dissolution rate varies between zero and the maximum dissolution rate, D , depending upon distance from equilibrium. They also assumed that the dissolved load is removed as quickly as it is formed, which is equivalent to assuming that mixing of water of different ages is negligible. To generalize their model from 1st order to n th-order reactions, one can let the forward reaction be equal to DA [mol/s] where A [m²] is the reactive surface area, and let the back reaction be equal to $DA (C/C_s)^n$ where n [dimensionless] is the order of the reaction, C [mol/m³] is the concentration and C_s [mol/m³] is the concentration at saturation. The load, L [mol/s], would then be equal to the balance of the forward and backward reactions:

$$L = DA[1 - (C/C_s)^n] \tag{3}$$

Assuming that the dissolved load is removed as quickly as it is formed, one can also write:

$$L = Q(C - C_o) \tag{4}$$

where C_o [mol/m³] is the initial (i.e. rainfall) concentration, C [mol/m³] is the final concentration and Q [m³/s] is the discharge. For first- and second-order reactions ($n = 1$ or 2 , respectively), Equations (3) and (4) can be solved for C as a function of Q :

$$\text{(for } n = 1) \quad C = \frac{DA + QC_o}{Q + DA/C_s} \tag{5a}$$

or

$$\text{(for } n = 2) \quad C = \frac{Q - \sqrt{Q^2 + \frac{4DA}{C_s^2}(DA + QC_o)}}{-2DA/C_s^2} \tag{5b}$$

where the negative root for $n = 2$ gives the concentration that has physical meaning. Using these equations and the observed concentration–discharge relationships, one can determine the values of DA , C_s and C_o that are required to fit the data. With three adjustable parameters, the model approximately reproduces the observed concentration–discharge relationship with either $n = 1$ or $n = 2$, although the log–log relationship is curved rather

than linear (Figure 5c). The order of the reaction does not strongly affect the overall quality of fit, but the dissolution rate times area (DA) parameter for the best-fit 2nd order scenario differs from the 1st order case. One cannot distinguish among models of different reaction order given only concentration–discharge data; additional *a priori* information about the order of the reaction or the dissolution rate and reaction area is needed to distinguish among the models. The best-fit saturated concentration is lower than the observed maximum concentration and the best-fit initial concentration is higher than the observed minimum concentration; the best-fit concentrations vary little as reaction order changes. In either case, the best-fit initial concentration is usually much higher than is realistic for rainfall. Rather than representing rainfall, the best-fit C_o probably reflects solutes acquired during infiltration through the soil column before reaching the groundwater system. Although multiple versions of the Langbein and Dawdy model fit the data reasonably well, the key assumption that there is no storage of water between storms and therefore negligible mixing of water of different ages is generally not valid (e.g. Buttle, 1994).

Permeability-porosity-aperture model

Here we suggest another model that is the only general model that we know of that produces a power–law relationship between concentration and discharge, assumes a variable solute flux that is proportional to the reactive surface area, and allows for mixing of waters of different ages. This final point distinguishes this model from the Langbein–Dawdy model.

The full derivation is shown in the appendix. The key assumptions are that permeability, porosity and average pore aperture or width, all decrease exponentially with depth; that Darcy’s Law describes flow through the catchment; that the effective precipitation rate is approximately spatially uniform across a hillslope; that flows originating near the divide and stream are minimal; and that solute flux is proportional to reactive surface area such that secondary and back-reactions do not control solute fluxes.

One can show that under these assumptions, the volume-weighted mean concentration (\bar{C} , [mol/m³]) draining a one-dimensional hillslope will be a power function of the water flux (Q_w),

$$\bar{C} = a_o Q_w^{b_o}, \quad b_o = \left(\lambda_k / \lambda_\phi - \lambda_k / \lambda_p - 1 \right) \tag{6}$$

where the constant a_o is a function of solute and catchment characteristics, and the power-law exponent b_o (dimensionless) depends on the rate at which permeability, porosity and pore aperture decrease exponentially with depth in the subsurface (represented by the e-folding length scales λ_k , λ_ϕ and λ_p , all in [m]). Because λ_k , λ_ϕ and λ_p are geometric properties of the subsurface and are not specific to individual solutes, equation (6) implies that b_o should be the same for all weathering-derived solutes at an individual site (see, for one example,

Figure 5d showing Ca at Andrews Creek). We fitted a single value of b_0 for each site, and a value of a_0 for each site and solute, using a non-linear fitting algorithm that minimizes the error between the modeled and observed concentrations for all solutes simultaneously.

Because we fit some models to all the solutes simultaneously whereas we fit other models to each solute independently, comparing the models is not a straightforward exercise. Using the AIC or BIC, or by looking at the example in Figure 5, it is clear that the Langbein-Dawdy model (5b) outperforms the simple mixing model (5a). The permeability-porosity-aperture model (5d) outperforms the Hubbard Brook Experimental Forest 'working model' (5c) according to the AIC and BIC at each of the eight featured sites. Comparisons between the Langbein-Dawdy and permeability-porosity-aperture model cannot be made using the AIC or BIC because the models are based on different sets of data (fitting each solute independently vs. all solutes simultaneously). Regardless of model performance, a key test of each of these models is whether the best-fit parameters make physical and chemical sense in the real-world catchments in which they are applied.

Contrary to the prediction of the permeability-porosity-aperture model, that the log-log slope b_0 of the concentration–discharge relationship should be the same for different weathering products at an individual catchment, the $\log(C)$ – $\log(Q)$ slopes for different solutes at the same site often differ by more than their uncertainties. This result could be explained by different depth profiles in the abundances of different minerals (and thus their reactive surface areas per unit pore surface). Mathematically this could be represented as λ_p taking on different values for different solutes, although this would imply that p would reflect not only pore aperture but also the relative abundances of different minerals. However, because b_0 is usually close to zero for different solutes, it is possible that the variation in λ_p may be small. Another parameter, b_1 , has been shown to relate storage and discharge in catchments, and is expressed as a function of the parameters λ_k and λ_ϕ (Kirchner, 2009; and see Appendix, Equation A12 and A13). The two log-log slopes b_0 and b_1 are not sufficient to uniquely constrain the three parameters λ_k , λ_ϕ and λ_p , so the individual e -folding depths (as well as values of the reactivity parameter k_R for each solute, see Appendix) could only be determined by direct measurement. Any such attempt at direct measurement, however, would be complicated by the spatial heterogeneity in subsurface properties, as well as the large differences between field and laboratory weathering rates (Schnoor, 1990; Brantley, 1992; White *et al.*, 1996).

The mechanism proposed here is in some ways analogous to that proposed by Clow and Drever (1996) to explain the relatively constant concentrations of weathering products in runoff from an alpine soil under widely varying rainfall. Clow and Drever (1996) argued that Si concentrations in their study catchment may be controlled by flushing and diffusion from micropores and seasonal

precipitation/dissolution of metastable amorphous aluminosilicates. They argued that because both flushing and reaction rates increase with increasing discharge, this combination of mechanisms would allow concentrations to remain relatively constant with fluctuating discharge. But whereas Clow and Drever (1996) argued that the rate of Si dissolution from the mineral phase should be controlled by Si concentrations in solution (and thus by the fluid flushing rate), here we assume that silicate weathering reactions are always far from equilibrium and thus are unaffected by changes in solute concentrations. Instead, in the permeability-porosity-aperture model outlined in Equation 6 and in the appendix, reaction rates increase at higher discharges because the wetted mineral surface area increases. Others have also argued that because Si is retained by secondary minerals to varying degrees, its concentration may be controlled in large measure by equilibration with respect to the secondary minerals that form (Drever and Clow, 1995; Godderis *et al.* 2006). Secondary mineral formation should preferentially affect Si and may explain why the power-law concentration–discharge slopes for Si are generally shallower than for the other major weathering products. These examples illustrate that different mechanisms can potentially generate similar observed concentration–discharge relationships, so it is important to verify the site-specific plausibility of any proposed mechanism.

FURTHER POSSIBILITIES

Many catchment-based chemical weathering models, such as Birkenes, ETD (Enhanced Trickle-Down), ILWAS (Integrated Lake Watershed Acidification Study), PROFILE/SAFE (Soil Acidification in Forested Ecosystems), MAGIC (Model of Acidification of Groundwater in Catchments), or WITCH [see review in Nordstrom (2004), pp. 60–62; Godderis *et al.*, (2006)], and other mineral weathering models such as PHREEQC (Parkhurst and Appelo, 1999), allow the simulation of weathering processes. We do not use these models in this study because most of our sites have insufficient information to apply them. Instead we explore in this paper whether a simple general modeling approach is possible based primarily on the observed concentration–discharge relationship. We show that several simple models can fit the observations well, but often they require unrealistic or internally inconsistent parameter values. Because data limitations have precluded us from testing more complex models, we cannot say whether their added complexity, and additional data requirements, would be helpful in understanding catchments' concentration–discharge behaviour. Future studies could also examine the geomorphic features, soil or regolith depth, presence of organic matter, or perennial/ephemeral status of the catchments, which may control weathering rates or fluxes in some catchments (e.g. Drever, 1994; Oliva *et al.*, 1999; Johnson *et al.*, 2001). These characteristics have not been considered in this study.

The relative constancy of concentrations across wide ranges of discharge requires solute production or solute mobilization at rates nearly proportional to the water flux. Depending on the relationship between reaction times and water transit times, one can infer the relative importance of production and mobilization. Based on field experiments, reaction rates have sometimes been inferred to be fast enough that the time to equilibrium is much shorter than average water transit times, such that waters are effectively always near equilibrium (e.g. Anderson and Dietrich, 2001). Buttle (1994) and many others have documented that most water reaching a stream during a storm event is so-called 'old' (i.e. pre-storm) water. Mean transit times in many catchments are on the order of ~ 1 year (McGuire and McDonnell, 2006, Table I), so this 'old' water may be near equilibrium with respect to certain minerals, with the consequence that solute fluxes mobilized by this 'old' water must be nearly proportional to water flux. However, studies of silicate weathering have typically found that reaction rates are slow (even relative to mean transit times of a year) and have assumed that catchments are kinetically-limited systems (see discussion in Brantley, 2004). Because the chemical weathering kinetics of silicates and carbonates differ (e.g. Brantley, 2004), one might expect different $\log(C)$ - $\log(Q)$ behaviour or explanatory models for catchments dominated by the distinct lithologies. However, for most of the solutes considered, the concentration–discharge slopes are not significantly different between the different lithologic settings. This suggests that differences in lithology and in reaction kinetics between carbonates and silicates do not significantly alter the relationship between concentration and discharge across the study sites. Time to equilibrium in the laboratory for mineral–water equilibrium reactions has been reported as a week to a year or longer (e.g. Bricker, 1968; Langmuir, 1997, Table 2.1) and field rates are even slower (Schnoor, 1990; Brantley, 1992; White *et al.*, 1996). This suggests that mineral weathering reactions would be unlikely to stay close to equilibrium, particularly during high flows. Determining the average time to equilibrium in the field is challenging: flow paths are heterogeneous and reactions and reactive surface areas are difficult to define. Nonetheless, as the preceding discussion illustrates, there would be much to be gained from determining how close weathering reactions are to equilibrium in the field.

IMPLICATIONS

Because concentrations are relatively constant with discharge across these diverse study catchments (Figures 1 and 2), solute fluxes (defined as concentration times discharge) from these catchments change nearly proportionally to discharge, both on an event basis and on an inter-annual basis (e.g. Figure 6). Although our observations are drawn from US catchments, these results are likely to be broadly generalizable because the HBN catchments include a broad range of climatic and lithologic

environments (Table I). A similar relationship between concentration and discharge is also seen in granitic boreal catchments in permafrost regions of Russia (Zakharova *et al.*, 2005), suggesting these observations and implications may be globally applicable. Climate change may substantially alter stream flows (especially if precipitation and evapotranspiration change in opposite directions). Such hydrologic changes will have little effect on concentrations but will alter fluxes almost proportionally.

Alkalinity flux to the ocean can be estimated as the sum of the Ca and Mg concentrations (McSween *et al.*, 2003, p. 147), or the hardness of the water. Raymond and Cole (2003) used this approach to estimate alkalinity for the Mississippi River for years before 1973 using hardness. They showed that overlapping alkalinity and carbonate hardness (=total hardness – noncarbonate hardness) measurements are accurate to $99.8 \pm 0.8\%$. Thus, we can estimate alkalinity fluxes based on the relationships between Ca, Mg and discharge presented in Figures 2 and 4. Raymond and Cole (2003) found that discharge and alkalinity flux in the Mississippi River increased by approximately 44% and 70%, respectively, over 48 years (1953–2001), attributed partially to changes in climate as well as changes in cropping patterns and additions from groundwater pumping. Based on the patterns in Figure 6 (and similar results for other solutes), one would expect solute flux from most watersheds across North America to vary nearly proportionally to water fluxes. Unlike the Mississippi River, most of the streams and rivers in the HBN are minimally affected by land use change or large amounts of groundwater pumping. Nonetheless, the nearly chemostatic behaviour demonstrated across so many diverse sites implies that alkalinity flux is largely determined by stream discharge. Streamflows at high latitudes are expected to increase by 10 to 40% over the next century, according to the latest report of the Intergovernmental Panel on Climate Change (IPCC, Core Writing Team, 2007). For a 10% increase in average annual flows, we would expect an approximately proportional 10% increase in alkalinity fluxes to the oceans. Carbonic acid weathering is one of the main mechanisms generating alkalinity; thus, an increase in alkalinity fluxes implies a concomitant increase in CO_2 consumption.

On the other hand, if discharges were to drop sharply, solute fluxes would also be expected to decrease. As an example, the seaward total dissolved solids flux from the Huanghe (Yellow) River, China has decreased by more than half over the last approximately 40 years because of a sharp decrease in water discharge in the lower reaches of the river (Chen *et al.*, 2005). Diversions, irrigation and reservoir use are primarily responsible for the decrease in water discharge, and despite an increase of ~ 5 to 10 mg/l/year in total dissolved solids in the middle and lower reaches of the river, there has been an overall decrease in solute flux (Chen *et al.*, 2005). Climate change models predict that flows in the southwestern United States and other dry areas are likely to decrease by 10 to 40% by 2090–2099 relative to 1980–1999 in a

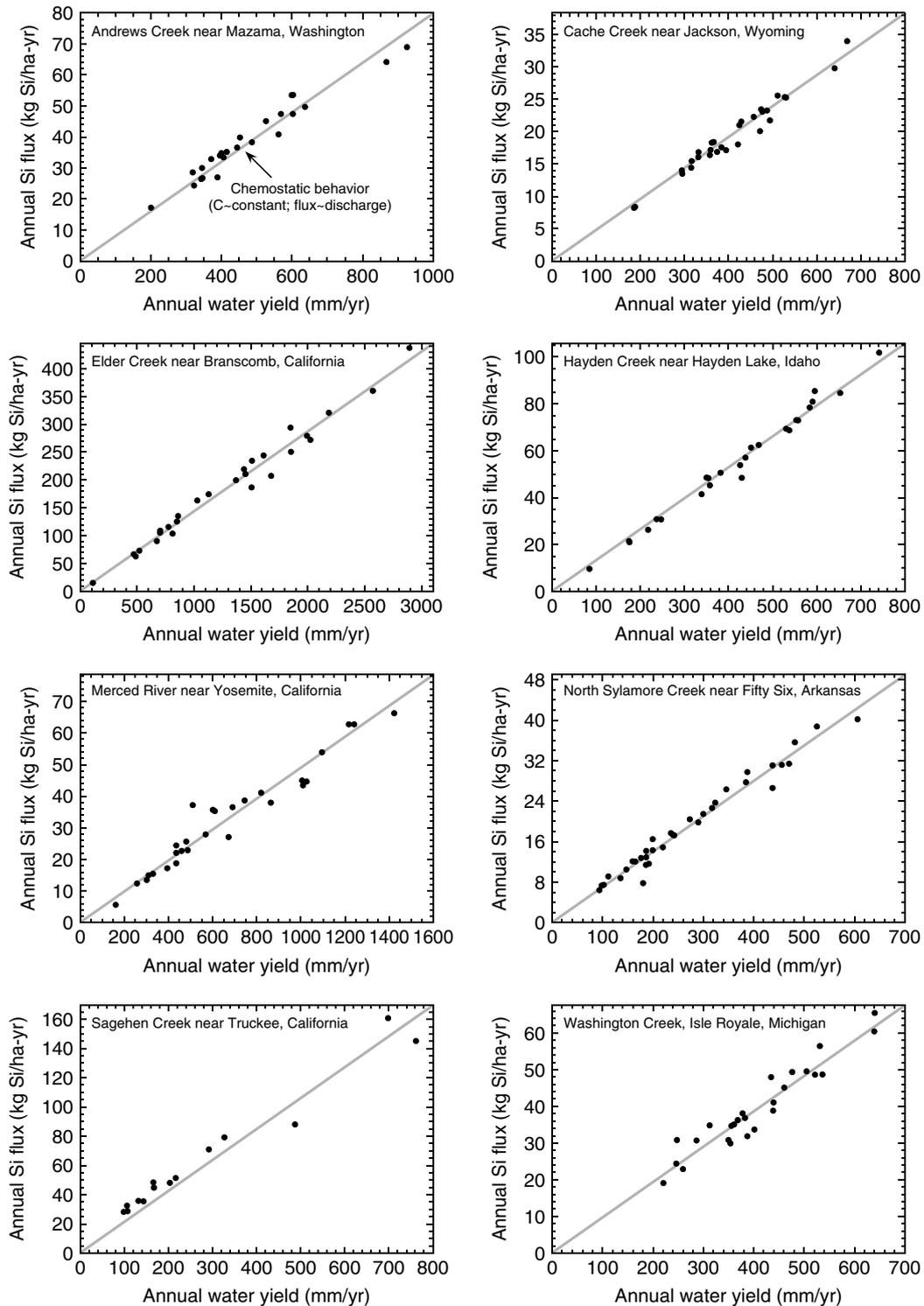


Figure 6. Annual silica fluxes in streamflow as a function of annual water yield for the eight Hydrological Benchmark Network streams shown in Figures 1 and 3. The diagonal grey line indicates solute fluxes proportional to discharge (i.e. constant concentration).

scenario in which global average temperatures increase by 2.8°C over the same period (IPCC, Core Writing Team, 2007). One would expect solute flux of the major base cations and silica from streams and rivers in these regions to decrease by an amount that is approximately proportional to the decrease in flows.

The stability of concentrations of weathering products across a wide range of flow regimes may be important

both for the health of individual organisms and for the diversity of aquatic ecosystems. At an organismal level, mortality from acidification-induced aluminum toxicity is closely linked to decreases in alkalinity and base cation concentrations (Jeffries *et al.*, 1992; Thornton and Dise, 1998). Metals and other contaminants are more toxic to juvenile fish in waters with lower hardness, which as noted above, is usually equal to sum of the concentration

of Ca and Mg (e.g. Hall, 1991). The greater the stability of base cation concentrations across a wide range of flows, the smaller the likelihood that toxicity thresholds will be crossed during hydrological extremes because concentrations will not drop precipitously when flows increase.

At a species to community level, site-to-site comparisons reveal that benthic macroinvertebrate and diatom species diversity is a function of total dissolved solid concentration, conductivity or salinity in some streams, lakes and fjords (Metzeling, 1993, Ryves *et al.*, 2004). Solute fluxes, especially the amount of Si relative to other potentially limiting nutrients, can be a predictor of phytoplankton blooms and diatom growth (LePape *et al.*, 1996; Grenz *et al.*, 2000). Si concentrations relative to concentrations of Fe, N and P strongly control diatom nutrient uptake and growth rates. Increased N and P concentrations relative to Si concentrations and decreased Si flux due to river regulation have shifted ecosystems dominated by siliceous phytoplankton or diatoms to those dominated by non-siliceous algae or flagellate communities (e.g. Officer and Ryther, 1980; Egge and Aksnes, 1992; Turner *et al.*, 1998; Billen and Garnier, 2007). Oceanic Si limitations have been seen in the eastern equatorial Pacific and North Atlantic as well as in coastal communities that have experienced eutrophication problems due to increased N and/or P loads relative to Si loads (Rague-neau *et al.*, 2000). Furthermore, rare taxa are more sensitive to changes in salinity than common taxa in site-to-site comparisons (Metzeling, 1993). Species that are more tolerant to salinity variations may be able to disperse widely into different rivers feeding an estuary or coastal region and negatively affect native populations, which may be adapted to the narrow range of concentrations seen in their particular chemostatic catchment (Bringolf *et al.*, 2005). Therefore, the chemostatic behavior of catchments may enhance hydrochemical stability across a wide range of flows and thus promote biodiversity, but also suggests that streams subject to anthropogenic salinity variations or estuarine influences are more vulnerable to invasive species.

CONCLUSIONS

Concentrations of weathering-derived solutes vary little with discharge for 59 USGS HBN streams, indicating that these catchments exhibit nearly chemostatic behaviour. Concentrations vary by only a factor of 3 to 20 as discharge varies by several orders of magnitude, and annual mean concentrations are similarly insensitive to changes in annual water yield. Concentrations of the major base cations and silica typically exhibit power-law relationships with discharge, with small negative exponents. Broad qualitative lithologic differences, such as the presence or absence of volcanics or carbonates, are associated with statistically significant differences in the power-law concentration–discharge slope among different sites. Other site characteristics such as

area, low temperature and average annual runoff are significantly rank-correlated with site-to-site variations in concentration–discharge slopes for some solutes, but the predictive power of site characteristics to quantify concentration–discharge slopes is limited. The narrow range of concentration variability with discharge implies that rates of solute production and mobilization must be nearly proportional to water fluxes. Because concentrations remain nearly constant across wide ranges in discharge, solute yield from catchments (and, at continental scale, alkalinity fluxes to the oceans) are predominantly determined by water yield.

It is difficult to find simple generalizable models that accurately represent the typical form of the concentration–discharge relationship, that are internally consistent, and that make plausible assumptions about catchment behaviour. A simple ‘bucket’ model cannot reproduce the observed concentration–discharge behaviour. The Hubbard Brook ‘working model’ can fit the observations, but the required best-fit ‘rainfall’ concentrations are much higher than observed concentrations, suggesting that key physical or chemical processes are not captured by the model. A Langbein–Dawdy chemical reaction model that assumes that reaction rates vary with distance from equilibrium can also fit the observed concentration–discharge relationships, but requires relatively high input concentrations (and therefore likely requires an important role for soil water) and assumes that no mixing of waters of different ages can occur. Finally, a new chemical and mixing model can explain the observed power-law relationships between concentration and discharge in terms of depth profiles of porosity, characteristic pore size and hydraulic conductivity in the catchment. In this model, changes in discharge correspond to changes in the depth of saturation in the subsurface. These in turn alter solute fluxes by altering the reactive wetted surface area. The assumptions of this new model should be tested at a subset of the HBN sites. An internally consistent model of hydrology, chemical weathering and transport is needed to explain the power-law concentration–discharge relationships that are observed across hydrochemically diverse catchments.

ACKNOWLEDGEMENTS

We thank Tom Meixner, Madeline Solomon, Steve Sebestyen, Jake Peters and Kathleen Lohse for their helpful discussions, and thank the 2003 Sagehen Watershed Symposium for stimulating the collaboration that led to this work. This work was supported by National Science Foundation (NSF) grant EAR-0125550, the Miller Institute for Basic Research in Science and an NSF Graduate Research Fellowship.

APPENDIX

Here we develop the new permeability-porosity-aperture model, briefly discussed in the main text, in which

chemical weathering and hydrological mixing jointly control the relationship between solute concentrations and water fluxes.

First, we assume that permeability (k , [m/s]), porosity (ϕ , [dimensionless]) and average pore aperture or width (p , [m]) all decrease exponentially with depth (z , [m]) from their values at the soil surface (k_o , ϕ_o and p_o , respectively):

$$k = k_o e^{-z/\lambda_k} \tag{A1}$$

$$\phi = \phi_o e^{-z/\lambda_\phi} \tag{A2}$$

$$p = p_o e^{-z/\lambda_p} \tag{A3}$$

The rates at which these variables decrease with depth, as expressed by the e-folding distances (λ_k , λ_ϕ , λ_p all [m]), do not need to be equal to one another. Permeability and porosity are known to decrease roughly exponentially with depth at many sites. An exponential decrease in aperture with depth is less well characterized, but this assumption is plausible and testable. Invoking Darcy's law with an approximately constant head gradient along the hillslope, and using Equation A1, one can express specific discharge (q , [m/s]) in a similar manner as an exponential function that varies as permeability decreases with depth:

$$q = q_o e^{-z/\lambda_k} \tag{A4}$$

where q_o is a reference discharge that equals k_o times the hillslope gradient. Thus water discharge (Q_w , [m²/s]) per unit hillslope width can be calculated as:

$$Q_w = \int_z^\infty q dz = \lambda_k q_o e^{-z/\lambda_k} \tag{A5a}$$

One can also assume that water discharge is proportional to effective precipitation inputs:

$$Q_w = Rx \tag{A5b}$$

where R [m/s] is the effective precipitation rate and x [m] is distance from the hill crest to any point along the hillslope. By setting Equations (A5a) and (A5b) equal to one another, one can solve for depth of the hydrologically active region (i.e. soil and bedrock) as a function of distance along the hillslope:

$$z(x) = -\lambda_k \ln \left(\frac{Rx}{\lambda_k q_o} \right) \tag{A6}$$

Equation A6 assumes that effective precipitation is spatially uniform along the hillslope and that flow originating near the divide and near the stream (i.e. in the non-linear portions of the hillslope) is negligible, and thus that the approximation of a constant hillslope gradient in Equation A4 is valid.

We can also define the solute flux per unit hillslope width (Q_s , [mol m⁻¹ s⁻¹]) so that it is proportional to the reactive surface area per unit land area, A_* [dimensionless]. Pore volume is the product of porosity

and total volume (V , [m³]), and reactive surface area per unit volume of pores and medium can be defined as

$$\begin{aligned} & \text{surf area}/(\text{volume of pores} + \text{medium}) \\ &= \frac{V\phi\gamma}{pV} = \frac{\phi\gamma}{p} \end{aligned} \tag{A7}$$

where γ [dimensionless] is a shape factor that is assumed to be constant with depth. We then integrate to get reactive surface area per unit land area, A_* :

$$\begin{aligned} A_* &= \int_z^\infty \gamma \frac{\phi}{p} = \int_z^\infty \gamma \frac{\phi_o}{p_o} e^{-z \left(\frac{1}{\lambda_\phi} - \frac{1}{\lambda_p} \right)} \\ &= \frac{\gamma\phi_o}{p_o \left(\frac{1}{\lambda_\phi} - \frac{1}{\lambda_p} \right)} e^{-z \left(\frac{1}{\lambda_\phi} - \frac{1}{\lambda_p} \right)} \end{aligned} \tag{A8}$$

Note that there is a larger wetted reactive surface area per unit land area, A_* , at higher flow rates in this model as a result of the relationship between z and R (Equation (A6)). For a surface dissolution reaction in which secondary and back-reactions can be ignored, solute flux per unit hillslope width (Q_s) is the product of the reaction constant, k_R [mol m⁻² s⁻¹], and the reactive surface area per unit land area, A_* , integrated along the linear segment of the hillslope from the base ($x = 0$) to near the ridge ($x = L$) using the relationships derived in Equations (A6) and (A8):

$$\begin{aligned} Q_s &= \int_0^L k_R A_* dx = \int_0^L \frac{k_R \gamma \phi_o}{p_o \left(\frac{1}{\lambda_\phi} - \frac{1}{\lambda_p} \right)} \\ & \quad e^{\left(\frac{\lambda_k}{\lambda_\phi} - \frac{\lambda_k}{\lambda_p} \right) \ln \left(\frac{Rx}{\lambda_k q_o} \right)} dx \\ &= \int_0^L \frac{k_R \gamma \phi_o}{p_o \left(\frac{1}{\lambda_\phi} - \frac{1}{\lambda_p} \right)} \\ & \quad \left(\frac{Rx}{\lambda_k q_o} \right)^{\left(\frac{\lambda_k}{\lambda_\phi} - \frac{\lambda_k}{\lambda_p} \right)} dx \\ &= \frac{k_R \gamma \phi_o}{p_o \left(\frac{1}{\lambda_\phi} - \frac{1}{\lambda_p} \right)} \left(\frac{1}{1 + \frac{\lambda_k}{\lambda_\phi} - \frac{\lambda_k}{\lambda_p}} \right) \\ & \quad \left(\frac{\lambda_k q_o}{R} \right) \left(\frac{Rx}{\lambda_k q_o} \right)^{\left(\frac{\lambda_k}{\lambda_\phi} - \frac{\lambda_k}{\lambda_p} + 1 \right)} \Bigg|_0^L \\ &= \frac{L k_R \gamma \phi_o}{p_o \left(\frac{1}{\lambda_\phi} - \frac{1}{\lambda_p} \right) \left(1 + \frac{\lambda_k}{\lambda_\phi} - \frac{\lambda_k}{\lambda_p} \right)} \\ & \quad \left(\frac{RL}{\lambda_k q_o} \right)^{\left(\frac{\lambda_k}{\lambda_\phi} - \frac{\lambda_k}{\lambda_p} \right)} \end{aligned} \tag{A9}$$

The volume-weighted mean concentration in the water flux (\bar{C} , [mol/m³]) is equal to the ratio of the solute flux (Equation A9) to the water flux (= RL), both expressed per unit hillslope width:

$$\bar{C} = \frac{Q_s}{Q_w} = \frac{\int_0^L k_R A_* dx}{Q_w}$$

$$\begin{aligned}
 &= \frac{Lk_R \gamma \phi_o}{p_o \left(1/\lambda_\phi - 1/\lambda_p\right) \left(1 + \lambda_k/\lambda_\phi - \lambda_k/\lambda_p\right)} \\
 &\quad \left(\frac{1}{\lambda_k q_o}\right) \left(\lambda_k/\lambda_\phi - \lambda_k/\lambda_p\right) (RL) \left(\lambda_k/\lambda_\phi - \lambda_k/\lambda_p - 1\right) \\
 &= a_o Q_w^{b_o} \tag{A10}
 \end{aligned}$$

A power-law concentration–discharge relationship can thus be expressed for a one-dimensional hill-

slope, with the constant a_o $\left[\text{mol} \cdot \text{s} \left(\frac{\lambda_k}{\lambda_\phi} - \frac{\lambda_k}{\lambda_p} - 1 \right) / \right]$ equal to all of the other constants

before the RL term, and the power-law exponent b_o [dimensionless] equal to:

$$b_o = \left(\lambda_k/\lambda_\phi - \lambda_k/\lambda_p - 1\right) \tag{A11}$$

Furthermore, storage (S , [m]) can be defined as the integral of porosity over total depth:

$$S = \int_z^\infty \phi = \lambda_\phi \phi_o e^{-z/\lambda_\phi} \tag{A12}$$

By combining Equations A5a and A12, one can see that discharge (Q_w) varies as a power function of storage:

$$Q_w/Q_o = (S/S_o)^{b_1} \tag{A13a}$$

where Q_o and S_o are reference values of discharge and storage, such that $Q_w = Q_o$ at $S = S_o$, and the power-law exponent, b_1 [dimensionless] is:

$$b_1 = \frac{\lambda_\phi}{\lambda_k}. \tag{A13b}$$

The value of b_1 can be determined from recession analysis, because Equation A13a implies that a plot of $-dQ_w/dt$ as a function of Q_w should have a log–log slope of $2 - (1/b_1)$, derived during periods when both evapotranspiration and precipitation are small relative to discharge (e.g. during rain-free nights) (Kirchner, 2009).

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