Abstract

Bands in volcanic rocks are deformed by inclusions, such as bubbles and crystals. The shape of deformed bands is compared with theoretical models for flow around inclusions. Deformation through either simple or pure shear can be distinguished for phenocrysts, but not bubbles. Studying band deformation at the microscale thus complements other textural measurements and structural approaches for reconstructing the kinematics and dynamics of lava flows.

1 Introduction

Flow banding is pervasive in silicic lava flows and domes. The use of the word “flow” in the term “flow band” implicitly implies that the geometry of bands is caused by deformation of the lava. Bands, such as those shown in Figure 1, can be defined by variations in bulk or trace element composition, crystallinity, or vesicularity. Several different processes can lead to the formation of bands, including magma mingling (e.g., Seaman, 1995; Perugrini et al., 2004), welding and rheomorphism (e.g., Stevenson et al., 1993), and repeated autobrecciation followed by reannealing (e.g., Smith, 1996; Gonnermann and Manga, 2003; Tuffen et al., 2003). From a kinematic perspective, the origin of the bands should not matter; what is more important is that the presence of bands provides a tracer to study lava deformation.

One common feature of flow bands is that they are deformed by inclusions, such as bubbles and crystals. This deformation should provide insight into the flow experienced by the bands. Similar structures develop from compaction, deformation, and recrystallization in metamorphic rocks and are reflected in foliations and lineations. In a metamorphic rock, to model the formation of structures, coupled equations for fluid and solid deformation as well as mass transfer between solid and fluid phases should be solved (e.g., McKenzie and Holness, 2000). In contrast, in lava, flow around
inclusions is governed by the much simpler problem of incompressible viscous flow.

Here I examine flow bands in obsidian to identify features of flow dynamics and kinematics that can be recovered from the deformation of bands through their interaction with inclusions in the lava. I show, for example, that it is possible to distinguish between pure and simple shear.

2 Samples

The obsidian samples studied in this article are from Obsidian Dome (California, USA), Little Glass Mountain (California, USA), and Rock Mesa (Oregon, USA). Obsidian Dome and Little Glass Mountain are effusive obsidian flows that erupted 0.5 ka yr BP (Miller, 1985) and 1.1 ka BP (Donnelly-Nolan et al., 1990), respectively. The Rock Mesa sample is from a 2.2 ka BP pyroclastic fall deposit on the flanks of South Sister Volcano, Oregon, USA (Scott, 1987).

Thin sections are cut parallel to the inferred flow direction and perpendicular the plane of banding. That is, flow bands define planes that are perpendicular to the thin section.

I focus on obsidian for two reasons. First, the optical transparency of the glass permits straightforward measurement and imaging of structures (Castro et al., 2003). Second, the concentration of crystals and bubbles is often sufficiently low that the interactions between the bubbles and crystals can be neglected, which greatly simplifies the quantitative analysis of preserved structures. The extension to flows with higher crystallinity, although in principle straightforward, requires both more challenging measurements (e.g., Gray et al., 2003) and more complex theoretical models to account for more complex rheology (e.g., Smith, 2000) and particle interactions (e.g., Arbaret et al., 1996).

3 Governing equations

We assume that, at the length scales for flow around the inclusions, deformation of lava is Newtonian. Flow is then governed by the Stokes equations

\[ \nabla p_d = \mu \nabla^2 \mathbf{u} \quad \text{and} \quad \nabla \cdot \mathbf{u} = 0 \quad (1) \]
with boundary conditions

\[ \mathbf{u} \to \mathbf{u}_{\text{ext}} \text{ as } \mathbf{x} \to \infty. \]  

(2)

Here, \( p_d \) is the dynamic pressure, \( \mu \) the fluid viscosity, \( \mathbf{u} \) the fluid velocity, and \( \mathbf{x} \) a position vector defined relative to the center of the inclusion, as shown in Figure 2. Bold symbols indicate vector and tensor quantities. The Newtonian approximation is reasonable provided strain rates are one to two orders of magnitude less than that for the glass transition (Webb and Dingwell, 1990), the relevant length scales of flow are comparable to or smaller than the distance between bubbles (Manga et al., 1998), and crystallinities are sufficiently low (less than 1% in this case) that they do not form an interconnected and rigid network (e.g., Saar et al., 2001).

Inclusions such as bubbles and phenocrysts provide obstacles to the free flow and deformation of magma. As a consequence, bands will be deformed around such inclusions, and the deformation of these bands depends on properties of the flow. We will assume that the external flow in equation (2), \( \mathbf{u}_{\text{ext}} \), is a linear flow; that is

\[ \mathbf{u}_{\text{ext}} = \mathbf{\Gamma} \cdot \mathbf{x} = \mathbf{E} \cdot \mathbf{x} + \frac{1}{2} \mathbf{\omega} \times \mathbf{x}, \]  

(3)

where \( \mathbf{\Gamma} \) is the velocity gradient tensor, \( \mathbf{E} \) is the rate-of-strain tensor, and \( \mathbf{\omega} \) characterizes the vorticity of the external flow. The solution for the flow velocity \( \mathbf{u} \) at position \( \mathbf{x} \) from the center of an isolated spherical particle or bubble can be derived most easily using vector harmonic methods (see, for example, Leal, 1992)

\[ \mathbf{u} = \mathbf{E} \cdot \mathbf{x} + \frac{1}{2} (\mathbf{\omega} \times \mathbf{x}) + \alpha \left( \frac{2\mathbf{E} \cdot \mathbf{x}}{5|\mathbf{x}|^5} - \frac{5\mathbf{x}(\mathbf{x} \cdot \mathbf{E} \cdot \mathbf{x})}{|\mathbf{x}|^7} \right) - \beta \frac{\mathbf{x}(\mathbf{x} \cdot \mathbf{E} \cdot \mathbf{x})}{|\mathbf{x}|^7}. \]  

(4)

For a bubble, \( \alpha = 0 \) and \( \beta = 1 \), and for a rigid sphere, \( \alpha = -1/2 \) and \( \beta = 5/2 \).

For completeness the pressure \( p \) and stress tensor \( \mathbf{T} \) are given, respectively, by

\[ p(\mathbf{x}) = p_{\text{ext}} - 2\beta \mu \frac{\mathbf{x} \cdot \mathbf{E} \cdot \mathbf{x}}{|\mathbf{x}|^5}, \]  

(5)

and

\[ \mathbf{T}(\mathbf{x}) = -p_{\text{ext}} \mathbf{I} + 2\mu \mathbf{E} + \alpha \mu \left[ 4 \frac{\mathbf{E}}{|\mathbf{x}|^3} - \frac{16}{|\mathbf{x}|^7} (2\mathbf{x}(\mathbf{E} \cdot \mathbf{x}) + 2(\mathbf{E} \cdot \mathbf{x})\mathbf{x} + (\mathbf{x} \cdot \mathbf{E} \cdot \mathbf{x})\mathbf{I}) + \frac{70}{|\mathbf{x}|^9} (\mathbf{x} \cdot \mathbf{E} \cdot \mathbf{x})\mathbf{x}\mathbf{x} \right] 
- 2\beta \mu \left[ \frac{\mathbf{x}(\mathbf{x} \cdot \mathbf{E} \cdot \mathbf{x})}{|\mathbf{x}|^5} - \frac{5}{|\mathbf{x}|^7} (\mathbf{x} \cdot \mathbf{E} \cdot \mathbf{x})\mathbf{x}\mathbf{x} \right]. \]  

(6)

Here \( p_{\text{ext}} \) denotes the pressure far away from the inclusion \( (\mathbf{x} \to \infty) \), and \( \mathbf{I} \) is the identity matrix.
For the illustrative examples considered next, we consider two end-member cases of linear flows: simple shear and pure shear. Because both the governing equations and external flow are linear, any combination of these flows can be superposed by linearly adding the solutions. For a simple shear flow, with \( \mathbf{u}_{\text{ext}} = (u_x, u_y, u_z) = (Gy, 0, 0) \), we have

\[
\mathbf{E} = \begin{pmatrix} 0 & G/2 & 0 \\ G/2 & 0 & 0 \\ 0 & 0 & 0 \end{pmatrix} \quad \text{and} \quad \omega = (0, 0, -G). \tag{7}
\]

For a two-dimensional pure shear flow, with \( \mathbf{u}_{\text{ext}} = (u_x, u_y, u_z) = (Gx, -Gy, 0) \), we have

\[
\mathbf{E} = \begin{pmatrix} G & 0 & 0 \\ 0 & -G & 0 \\ 0 & 0 & 0 \end{pmatrix} \quad \text{and} \quad \omega = 0. \tag{8}
\]

In the examples that follow, I show the expected shape of bands formed by flow around inclusions. The calculated bands are shown as sets of curves whose shape can be compared with actual bands. The calculated bands are determined by advecting material lines that initially start far from the inclusions and by following these material lines through the flow (that is, I integrate \( \frac{d\mathbf{X}}{dt} = \mathbf{u} \) where \( \mathbf{X} \) describes the position of a material line at time \( t \)). In the case of simple shear, calculated bands will be the same as streamlines.

### 4 Phenocrysts

Figure 3 shows deformed bands of microlites around a phenocryst in obsidian from Obsidian Dome. Also shown are streamlines for pure (solid curves) and simple (dashed curves) shear around a rigid sphere. For the case of simple shear, the sphere is allowed to rotate freely. Predicted band shapes for pure shear agree much better with the observed deformed bands. The difference between these two flows is greatest just upstream (and downstream) of the sphere, and for this reason, I only show predicted band shapes close to the sphere for the simple shear case. This sample was collected from the front of the flow in an obsidian layer located approximately midway between the base and surface of the flow. Here, flow is expected to be dominated by pure shear (Merle, 1998), as inferred from Figure 3. Castro et al. (2002) analyzed the orientation distribution of the microlites in Obsidian Dome and also concluded that flow in the same obsidian layer was probably dominated by pure shear.
Figure 4 shows oriented microlites around a phenocryst in obsidian from Little Glass Mountain. Also shown are calculated shapes of deformed bands for different proportions of pure and simple shear around a rigid sphere, assuming again that the sphere is free to rotate. The relative proportions of pure and simple shear changes from all pure shear (Figure 4a) to all simple shear (Figure 4c) with equal amounts of pure and simple shear in (Figure 4b). A qualitative comparison of the calculated and observed flow bands indicates a combination of pure and simple shear. The difference between the two end-members is most obvious close to the phenocryst, in the region often termed a “stress shadow”. This sample was collected from the front and near the base of the flow. At the very bottom of a flow, deformation is expected to be dominated by simple shear because of the no-slip boundary condition on the bottom of the flow. The relative amount of pure shear increases upward from the base (Buisson and Merle, 2004). The conclusion that some pure shear is preserved differs from my earlier analysis (Manga, 1998), in which I showed that the orientation distribution of microlites in the same sample is better explained by simple shear than by pure shear. One possible explanation for this discrepancy is that the orientation distribution of microlites developed in the conduit (where flow should be dominated by simple shear). Once on the surface, the pure shear associated with spreading is then more rapidly reflected in the band shapes than in the microlite orientations. The orientation distribution of microlites preserved in these rocks requires strains of $O(10)$ to develop. In contrast, strains of $O(1)$ are sufficient for band deformation to reliably indicate the type of flow.

5 Bubbles

Bubbles, unlike solid phenocrysts, may themselves be sources of flow if they grow as a result of exsolution or shrink because of resorption. The growth of bubbles within extruding silicic domes and flows is one way for bubbles to develop high vesicularities. Whether bubbles grow within the flow to make vesicular pumice with large bubbles (e.g., Fink et al., 1992) – the so-called coarse vesicular pumice – or bubbles are resorbed or collapse to make low-vesicularity obsidian (e.g., Eichelberger et al., 1986) has been the subject of some controversy.

The flow created by an expanding bubble, when the influence of other bubbles can be ignored, is given by

$$u(x) = \left( \frac{a}{|x|} \right)^2 \frac{da}{dt} e_x,$$  

(9)
where $a$ is the radius of the bubble and $\mathbf{e}_x$ is a unit vector in the same direction as $\mathbf{x}$.

Figure 5 shows deformed bands around a bubble in obsidian from Obsidian Dome. Also shown are the expected shapes of initially planar and parallel bands that are displaced outward by the growing bubble. The agreement between the observed and calculated band deformations suggests that this bubble grew after the bands were created, and thus presumably after emplacement of the flow.

Identical deformed bands, however, are also produced by both simple and pure shear around a spherical (nondeforming) bubble. The reason all these flows produce the same deformed bands is that the velocity field responsible for band deformation (i.e., the disturbance flow) in all cases is that created by a point force, or Stokeslet. The disturbance in the flow created by a rigid sphere, in contrast, is more complicated because of the no-slip boundary condition on the surface of the sphere, and it differs for pure and simple shear flows. As a consequence, for our spherical bubble, we can confirm that flow bands are indeed flow bands, in that they reflect flow and deformation, but we cannot be more specific about the nature of the flow without additional constraints.

6 Discussion

Bands are formed by deformation of ascending and flowing magma and thus preserve a record of this deformation. As with all geological structures, the geometry of the bands we are left to analyze reflects the integrated history of their formation and subsequent deformation, and some care and thought is needed to interpret any observations.

Here I considered only the deformation of bands by inclusions. The selected examples were chosen because they illustrate that it is possible to infer flow type (e.g., pure vs simple shear), at least when the concentration of inclusions is low. It is not, however, possible to use deformed bands to determine the magnitude of the strain rate and, at least for the examples shown here, the total strain. To determine strain, the initial shape and position of the material that defines the bands must be known.

To reconstruct the full kinematics and dynamics from structural and textural measurements
clearly requires other measurements. Table 1 provides a summary of the kinematic and dynamic properties (flow type, strain rate, total strain) that can be determined quantitatively from textural and structural studies. The symbols Y, N, and S indicate whether the listed structure can, cannot, or can only sometimes be used to determine the listed kinematic and dynamic properties. Deformed bubbles, because of the presence of surface tension stresses, can in some cases be used to determine either deformation rates or strain, as well as flow type (Coward, 1980; Polacci and Papale, 1997; Rust et al., 2003). Deformed enclaves provide constraints on total strain and flow type (Williams and Tobisch, 1994; Blake and Fink, 2000; Ventura, 2001), provided the rheology and formation of the enclaves are understood (Paterson et al., 2004). The preferred orientation of crystals, and the resulting fabrics, reflect both the flow type and total strain (e.g., Shelley, 1985; Wada, 1992; Ventura et al., 1996; Manga, 1998; Smith, 2002). Finally, the shape of folds can reflect the flow type and strain (e.g., Fink, 1980; Smith and Houston, 1994; Castro and Cashman, 1999), provided the rheology of the different layers in the fold is known (e.g., Biot, 1961; Schmalholz and Podladchikov, 2000). In table 1, I assign an S for strain inferred from bands, because if the initial conditions can be reconstructed, strain can then be inferred.

Table 1 shows that several sets of studies are needed to reconstruct flow dynamics and kinematics. Fortunately, Table 1 also shows that there is likely to be independent confirmation of inferences based on only one type of measurement. For example, in the examples shown in Figures 3 and 4, the orientation distribution of microlites provides an independent check on the flow type inferred from the deformed bands.

As a further example, in Figure 6a I show deformation of a band of oxide particles around a much larger clump of oxides in a sample of pyroclastic obsidian from Rock Mesa, Oregon. This obsidian is assumed to come from near the conduit wall, where flow is most likely dominated by simple shear (Rust et al., 2003). In Figure 6b, I superimpose a flow line for a simple shear flow around a sphere (representing the large clump of oxide particles) – the agreement is excellent indicating that flow was dominated by simple shear. Confirmation is provided by the deformed bubbles at the top of the image in Figure 6b; in simple shear, deformed bubbles are oriented at an angle to the flow direction. This angle depends on the degree of deformation (Rust and Manga, 2002), and the orientation of the bubble in Figure 6b is consistent with the flow direction that can be inferred from the line of oxide particles.
Figure 6b, however, also shows the expected shape of a band deformed by pure shear around the same clump of oxide particles. Its shape is nearly identical to the shape of the band formed in simple shear. As noted in §4, the difference between bands deformed in pure and simple shear is most apparent just upstream and downstream of inclusions. As a consequence, to interpret deformed bands, it is essential to focus on their shapes very close to inclusions.

7 Concluding remarks

The pattern of band deformation around solid inclusions provides constraints on the dominant style of flow experienced by the lava. Deformed bands around bubbles are not useful for quantifying dynamics and kinematics other than verifying the obvious: bands are indeed shaped by flow. Features other than deformed bands, such as deformed bubbles, enclaves, fabrics, and folds, provide complementary information about kinematics and dynamics. Integrating constraints from deformed bands can thus provide either new information or independent tests of inferences.
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Table 1: Flow attributes that can be quantified from different structures (S: sometimes; Y:yes; N:no)

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<thead>
<tr>
<th>Structure</th>
<th>Strain</th>
<th>Strain rate</th>
<th>Flow type</th>
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<tbody>
<tr>
<td>Bubbles</td>
<td>S</td>
<td>S</td>
<td>S</td>
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<tr>
<td>Enclaves</td>
<td>Y</td>
<td>N</td>
<td>Y</td>
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<tr>
<td>Crystals</td>
<td>S</td>
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<td>Folds</td>
<td>Y</td>
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<td>Y</td>
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<tr>
<td>Bands</td>
<td>S</td>
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Figure 1: Bands in obsidian from Big Obsidian Flow, Newberry Volcano (Oregon, USA). Scale bar is 1 mm long. The ellipsoidal inclusions are bubbles. The phenocryst in the lower right is feldspar. From Castro (1999).
Figure 2: Geometry of the model flow problem showing the inclusion (bubble or rigid sphere).
Figure 3: Bands in obsidian from Obsidian Dome deformed by a phenocryst. Predicted deformation of bands for pure shear (solid curves) and simple shear (dashed curved) around a rigid sphere (bold, solid semicircle). Deformation of bands is better explained by pure shear than simple shear.
Figure 4: A band deformed by flow around a phenocryst from Obsidian Dome, California, USA, showing changes in microlite orientation. Also shown in (a) are expected shapes of deformed bands (parallel to the expected orientation of microlites) for simple shear around a sphere. b) Predicted bands shapes for a flow that consists only of pure shear. c) Predicted band shapes for a flow that consists of equal parts pure and simple shear.
Figure 5: Predicted deformation of bands (red curves) around an expanding bubble. Identical band deformation is also produced by pure and simple shear around a spherical bubble. Sample is from Obsidian Dome, California, USA.
Figure 6: a) Line of small oxides particles deformed by flow around a large cluster of oxides particles. b) Predicted band shapes for simple shear (yellow) and pure shear (red) around a free-rotating sphere. b also shows deformed bubbles whose orientations, relative to the line of oxide particles, is consistent with a flow dominated by simple shear. Sample is from Rock Mesa, Oregon, USA (Rust et al., 2003).