

# A Rayleigh wave back-projection method applied to the 2011 Tohoku earthquake

Daniel Roten, Hiroe Miyake, and Kazuki Koketsu (2012), *GRL*

Earthquake of the Week - 27 January 2012

# Motivation and Summary

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Region of maximum slip in recent source inversions of 11 March, 2011

$M_w$  9.1 EQ strongly data-dependent:

- Near trench [e.g. Lay et al., 2011; Pollitz et al., 2011]
- Near JMA hypocenter [e.g. Ammon et al., 2011; Simons et al., 2011]
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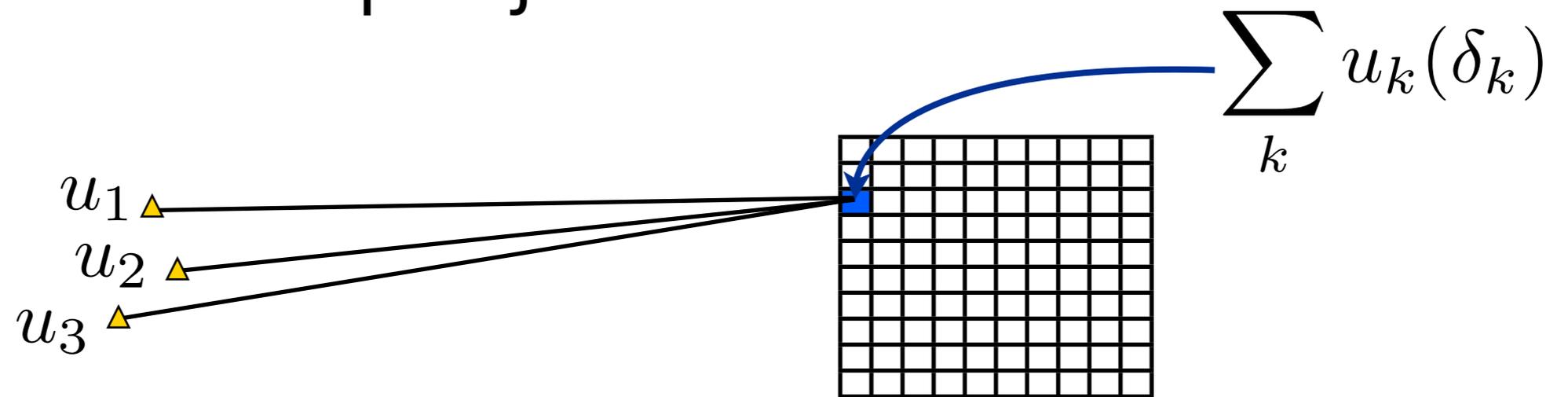
Up-dip extent of rupture overall difficult to assess [e.g. Lay et al., 2011]

*Authors suggest frequency-dependent radiation as potential explanation [e.g. Koper et al., 2011]*

*Employ multi-frequency ( $T=13-100$  s) surface-wave back projection in order to assess this effect*

Methods: Back projection

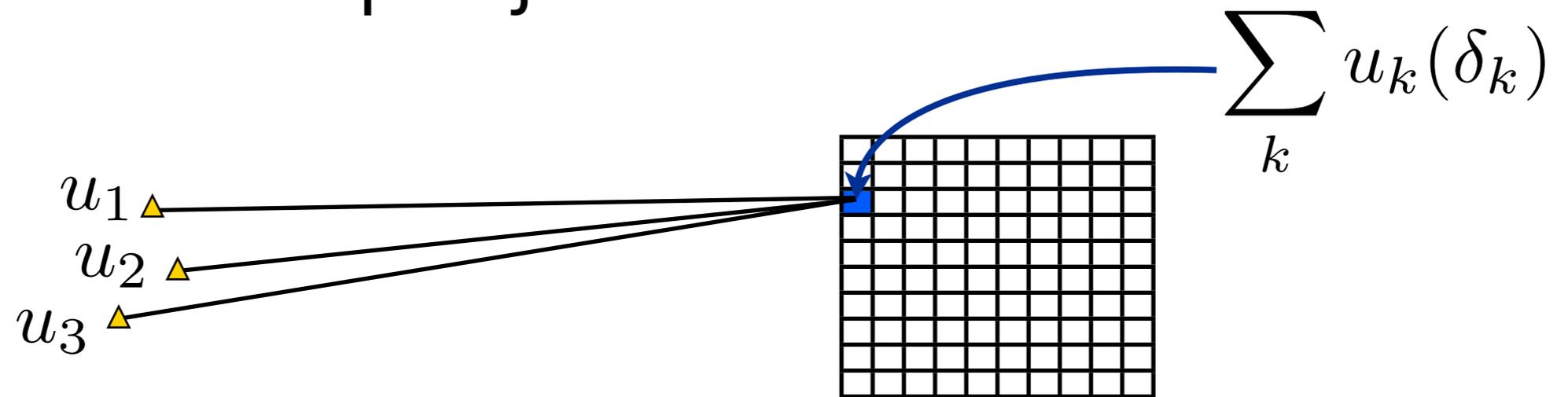
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Given grid of potential source locations, identification by waveform stacking and migration to predicted travel time of chosen phase

*Want:* highest amplitude phase, well-separated

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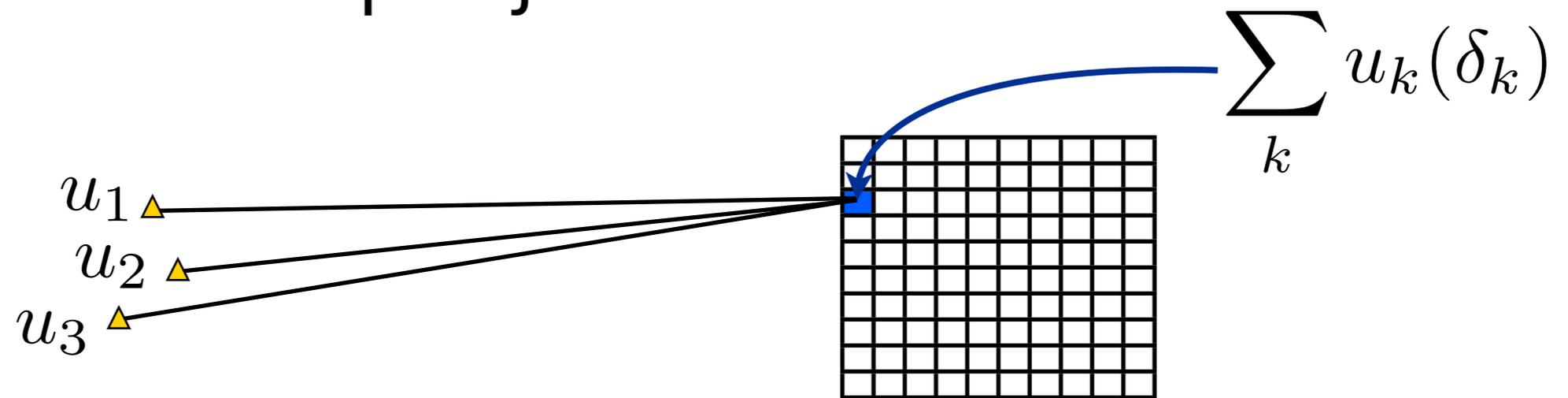
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P arrival used successfully for teleseismic body-wave BP, but local to regional distances difficult:

**Local distance:** little separation between P and stronger S

**Regional distance:** ( $>150\text{km}$ )  $S_n$  before direct  $S_g$ , followed by strong  $L_g$

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Authors use Rayleigh wave BP from K-NET and KiK-net recordings, as these phases are both *strong* and *dispersive*

Methods: *Waveform processing*

# Methods: Waveform processing

Authors use a continuous wavelet transform in order to isolate energy at the period of interest:

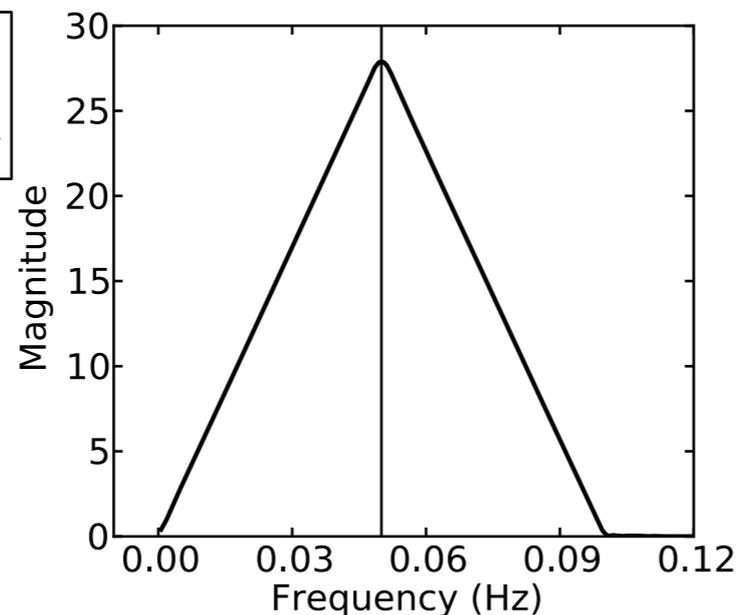
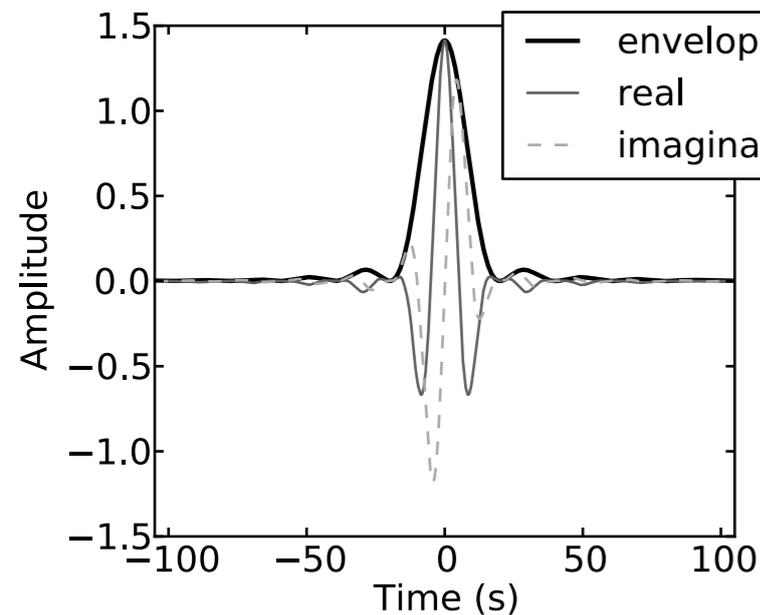
$$wt_k(s, \tau) = \frac{1}{\sqrt{s}} \int_{-\infty}^{+\infty} u_k(t) \psi^* \left( \frac{t - \tau}{s} \right) dt$$

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where  $\psi_B(t) = \sqrt{f_b} \left[ \text{sinc} \left( \frac{f_b t}{p} \right) \right]^p \exp \{ 2\pi i f_c t \}$



$f_b$  bandwidth

$f_c$  center

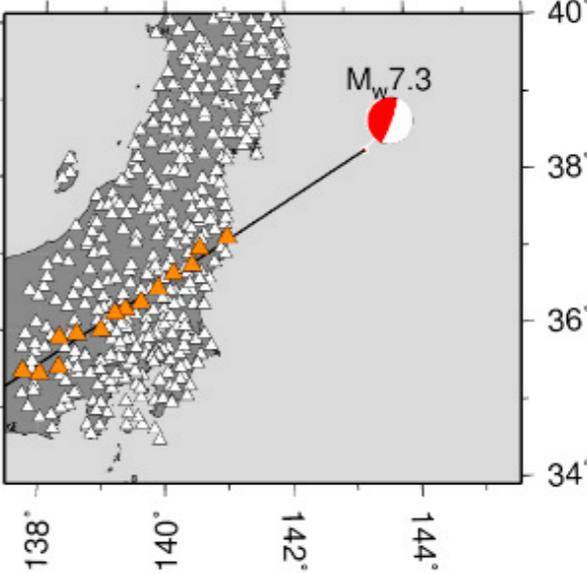
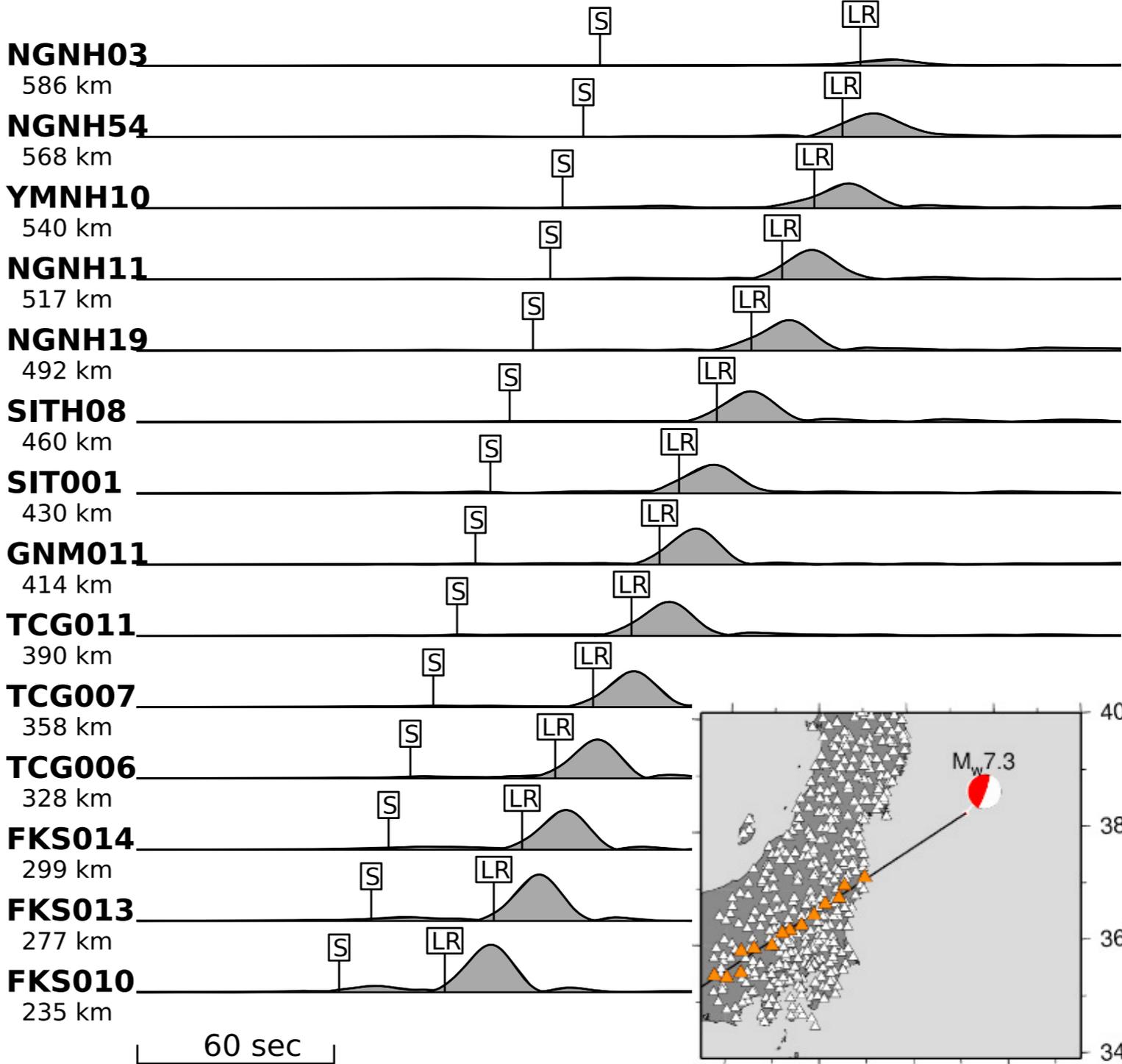
Chose 1 Hz center in mother wavelet - scale becomes period

# Methods: Waveform processing

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Synthetic (FD) example for vertical component waveforms of  $M_w$  7.3 foreshock ( $T=13s$ )

Rayleigh waves clearly visible as strongest phases in CWT envelopes



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$$S_m(s, \tau) = \left| \sum_{k=1}^N wt_k(s, \tau + \delta_{m,k}) w_{m,k} p_{m,k} \right|^2$$

Authors take square modulus of migrated, *weighted*, stacked waveforms

$s$  period

$\tau$  source time

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$w_{m,k}$  source-station azimuth weighting

$$\frac{1}{w_{m,k}} = \sum_{i=1}^N 1 - \frac{|\theta_{m,i} - \theta_{m,k}|}{\Delta\theta}$$

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$\delta_{m,k}$  Predicted travel time from group-velocity dispersion map

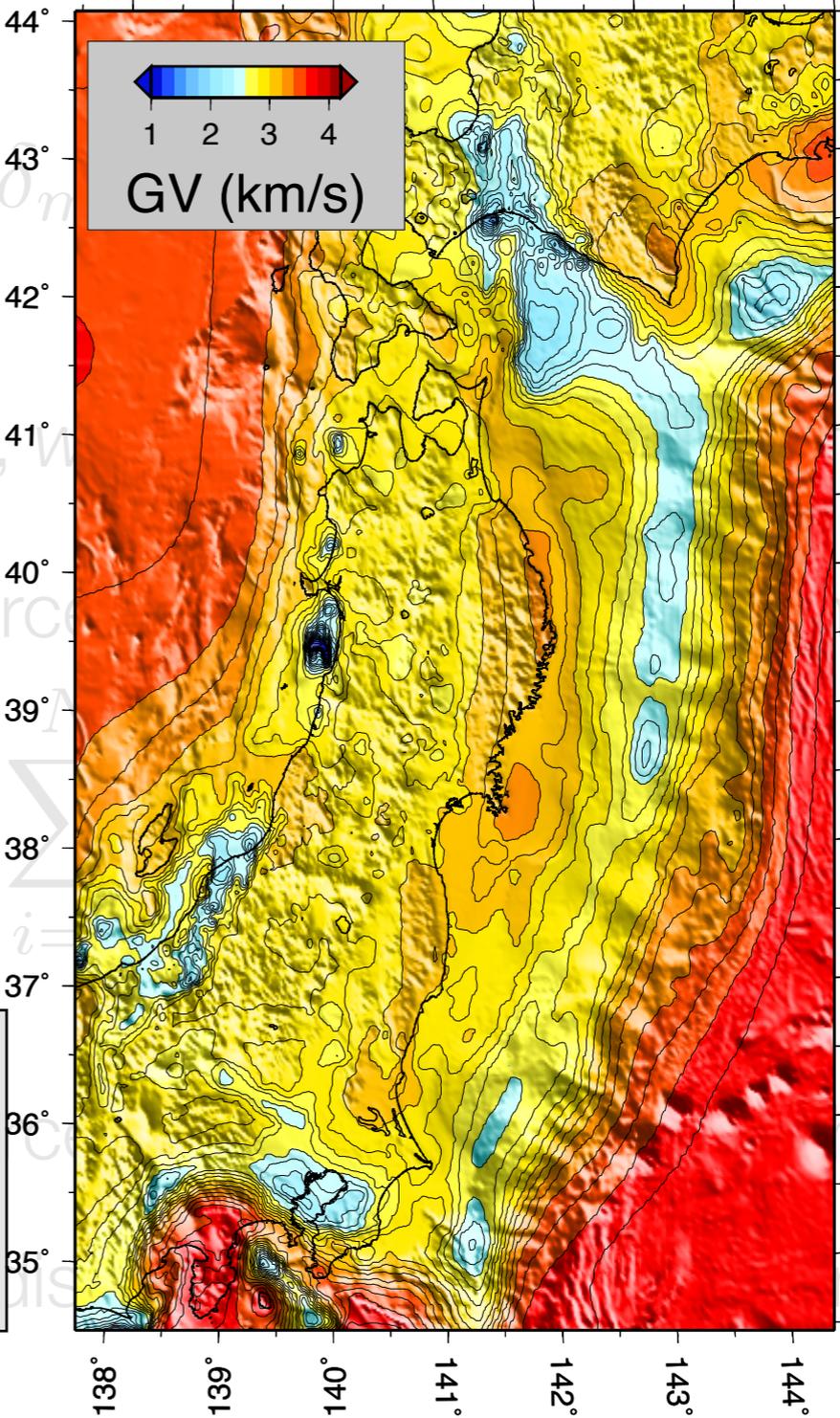
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$$w_{m,k} = \frac{1}{w_{m,k}}$$



**Right:** Fundamental-mode Rayleigh wave group velocities derived from the Japan Integrated Velocity Structure Model (JIVSM) [Koketsu et al., 2008] - here shown for T=20s.

$$\delta_{m,k}$$

Predicted travel time from group-velocity dispersion map

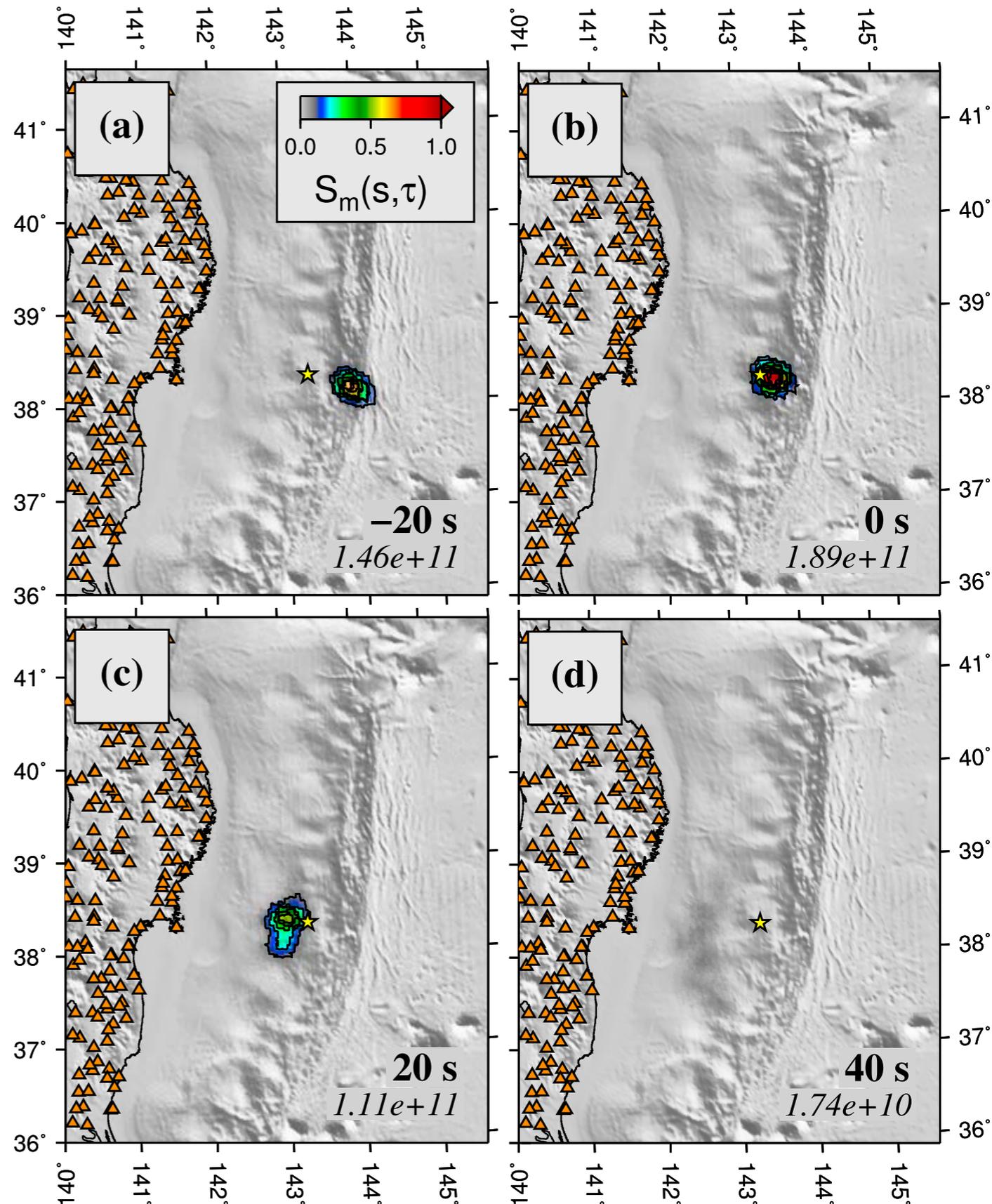
# Methods: Synthetic validation

FD simulation of Mw 7.3 foreshock as a point source in the Japan Integrated Velocity Structure Model [Koketsu et al., 2008]

Stack maximum at zero time and true location

Ghost peaks migrate from ESE to WNW

**At right:** BP of Mw 7.3 foreshock radial-component synthetics ( $T=20s$ ) using same 384 stations as in later study of Mw 9.1 mainshock



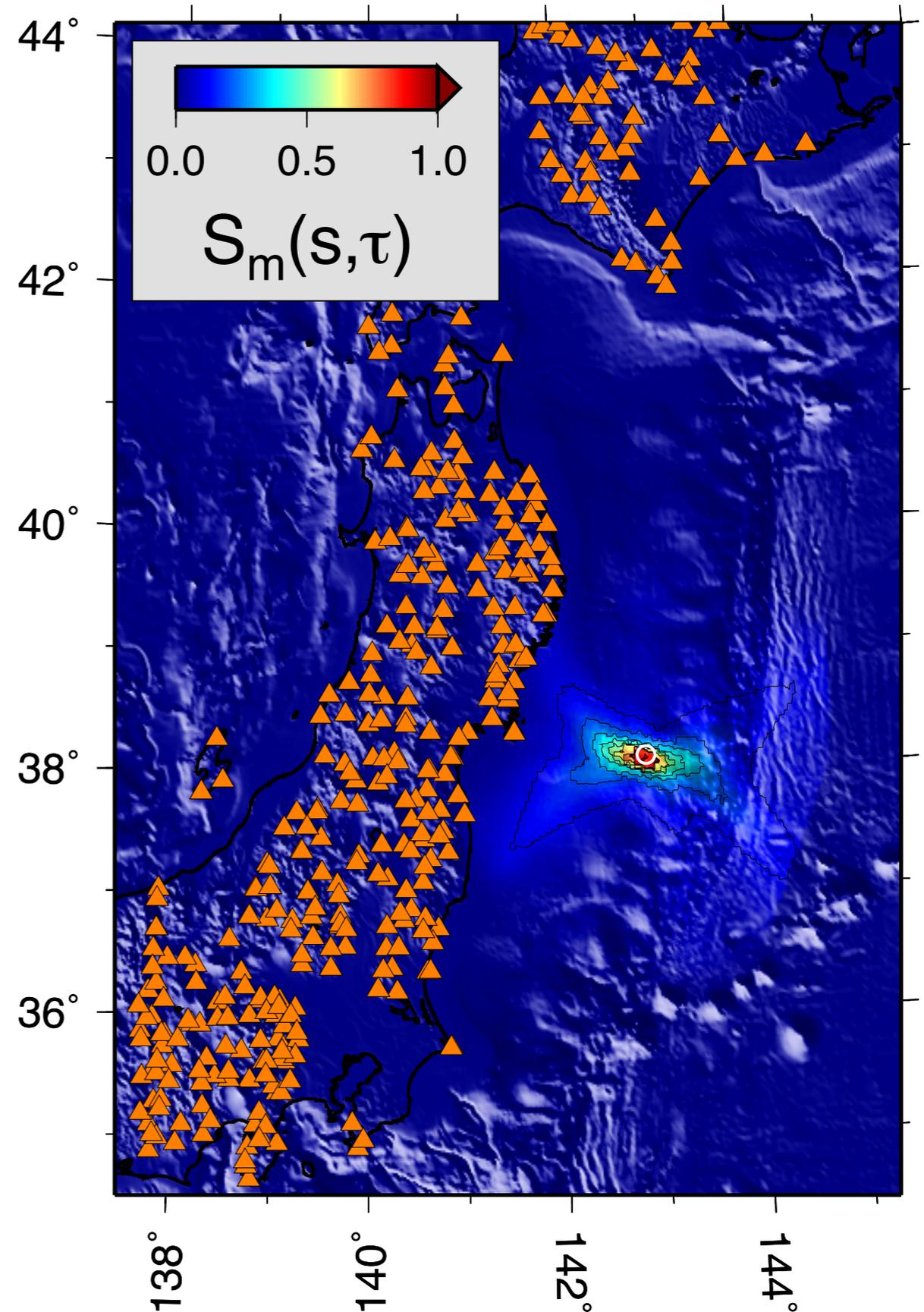
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**At right:**  $T=20$ s array response function  
estimate for the 384 K-NET / KiK-net  
stations used in mainshock BP.



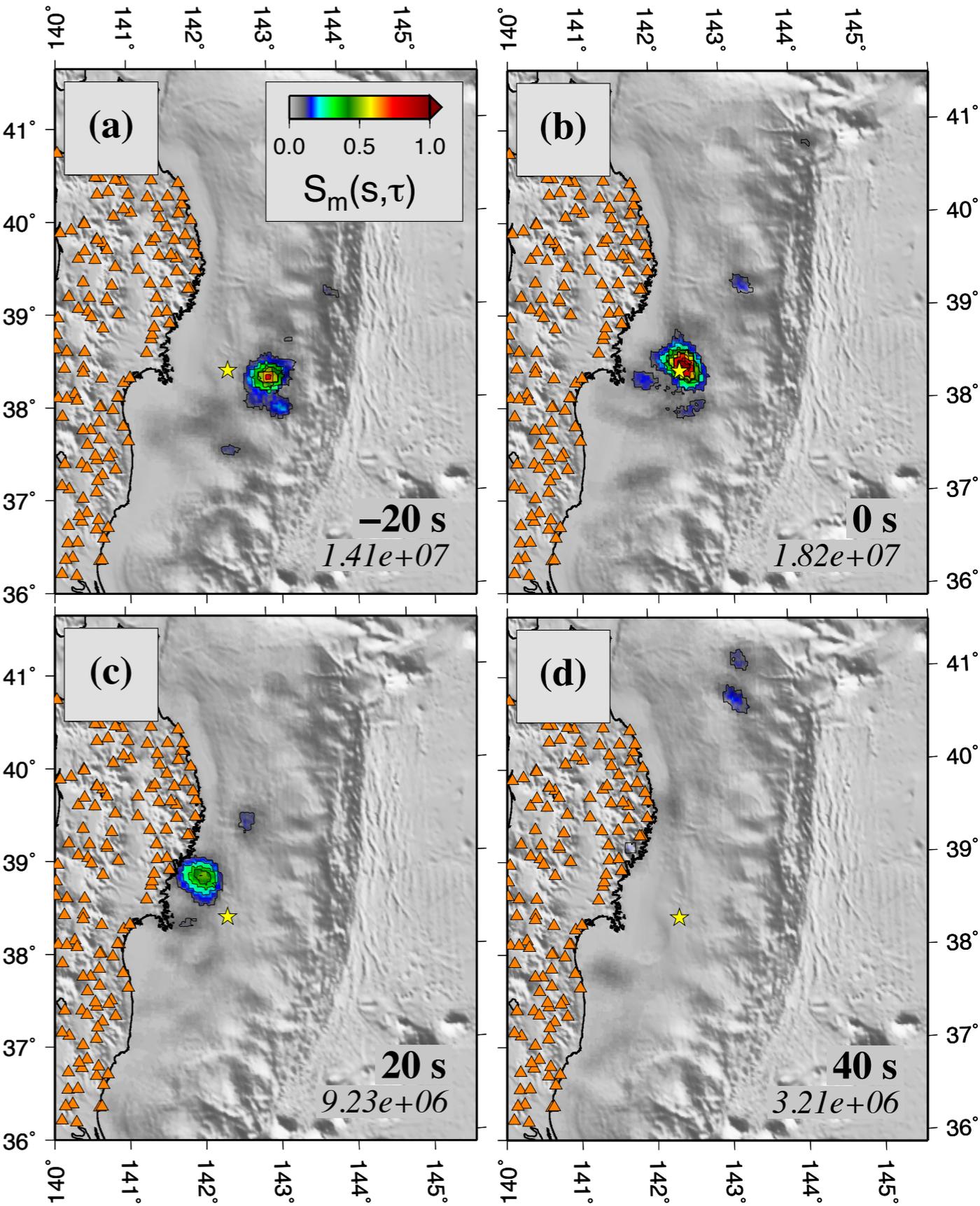
# Methods: Data validation

BP of Mw 6.5 aftershock of 28 March using 284 K-NET / KiK-net stations. Same behavior as in synthetic example.

Stack maximum at zero time and true location

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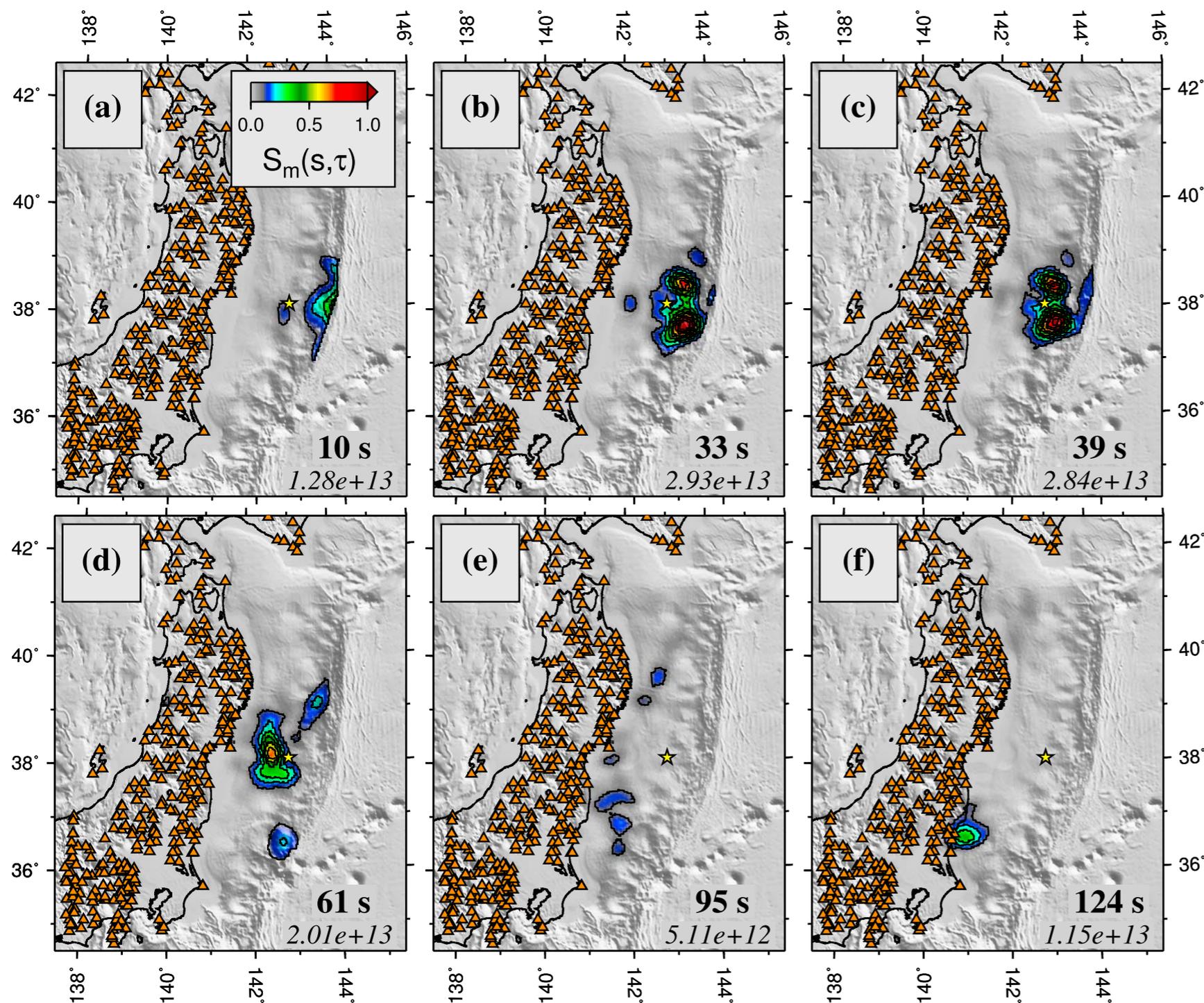
**At right:**  $T=13s$  BP result. JMA epicenter is yellow star.



# Application to the $M_w$ 9.1 mainshock

Authors performed Rayleigh-wave BP at 13, 20, 30, 50, and 100 s

Prefer a three-stage progressive rupture model



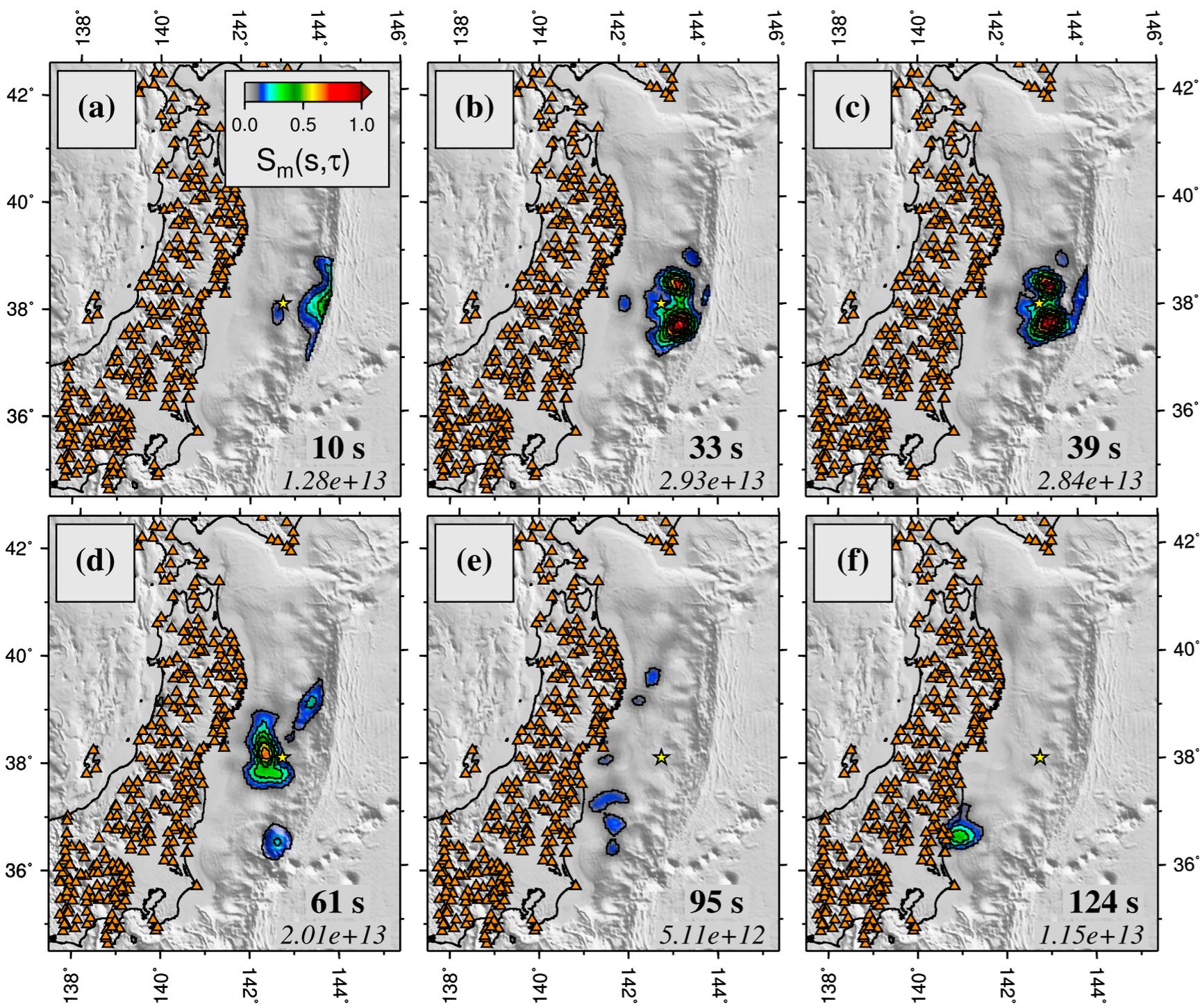
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**At left:** 20 s mainshock BP

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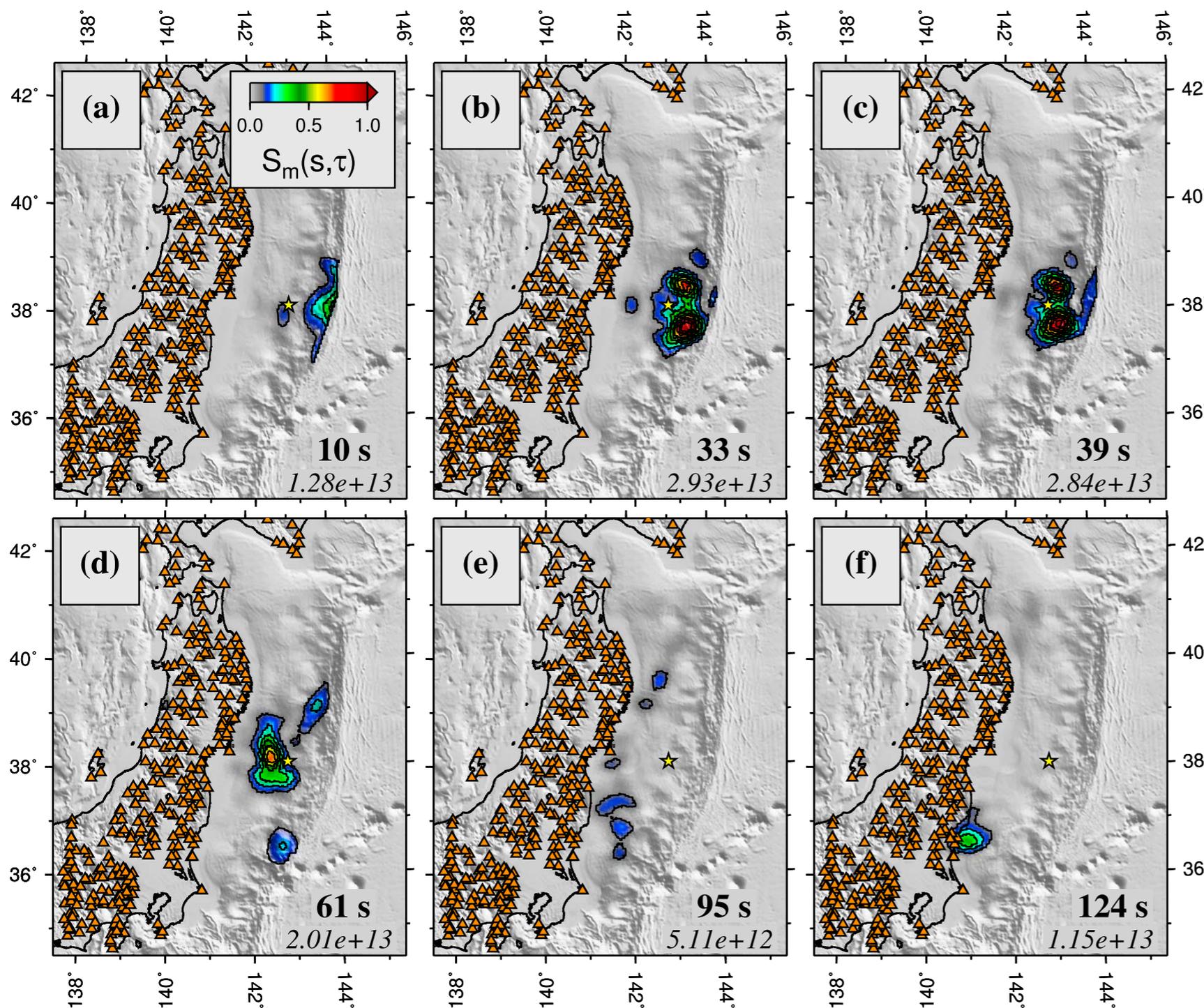
**Stage 2:** Dual peaks to SE (33 s) and NE (39 s)

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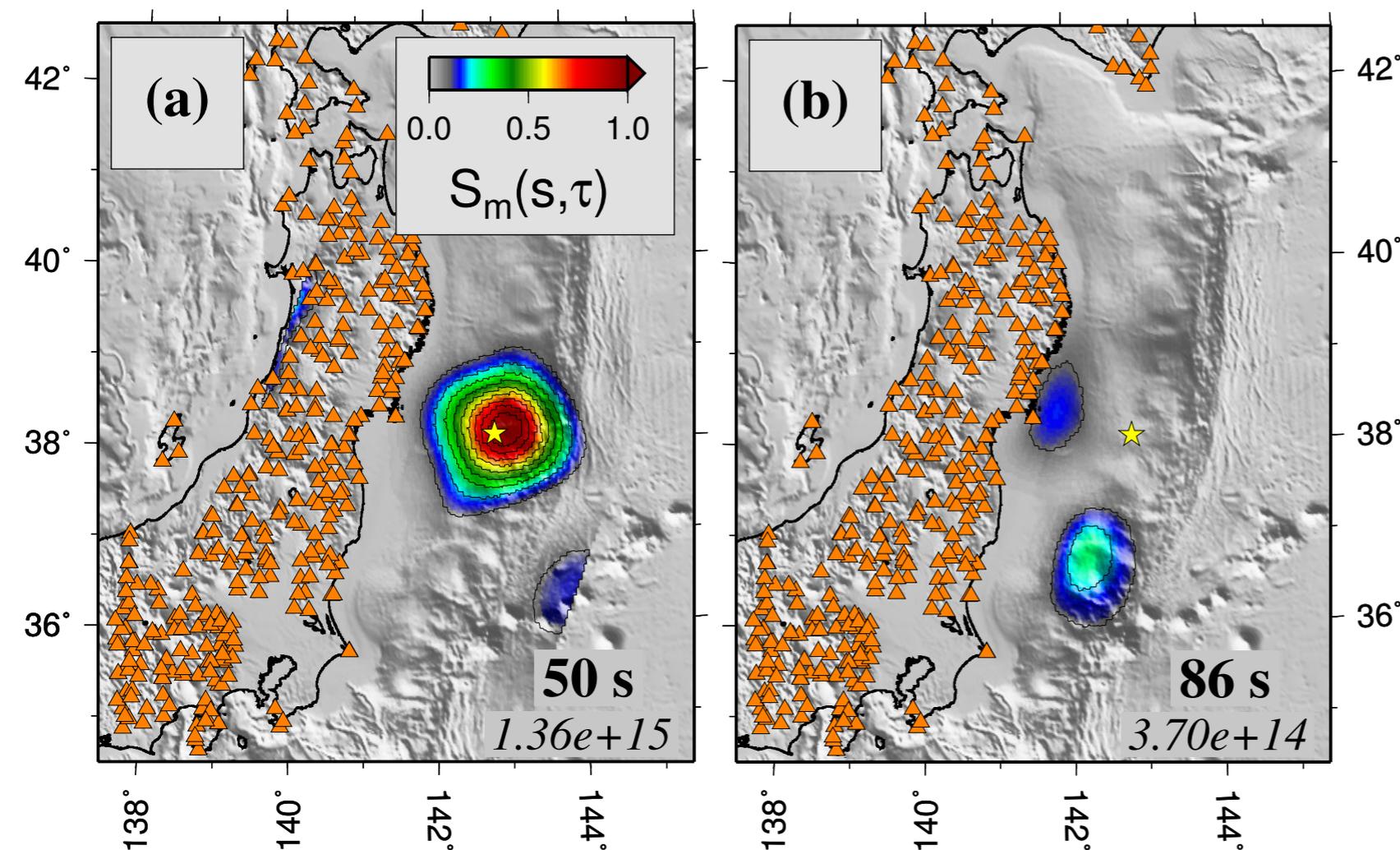
**Stage 3:** Northern segment peaks off Iwate at 61 s; Southern segment peaks at 124 s off near Fukushima-oki

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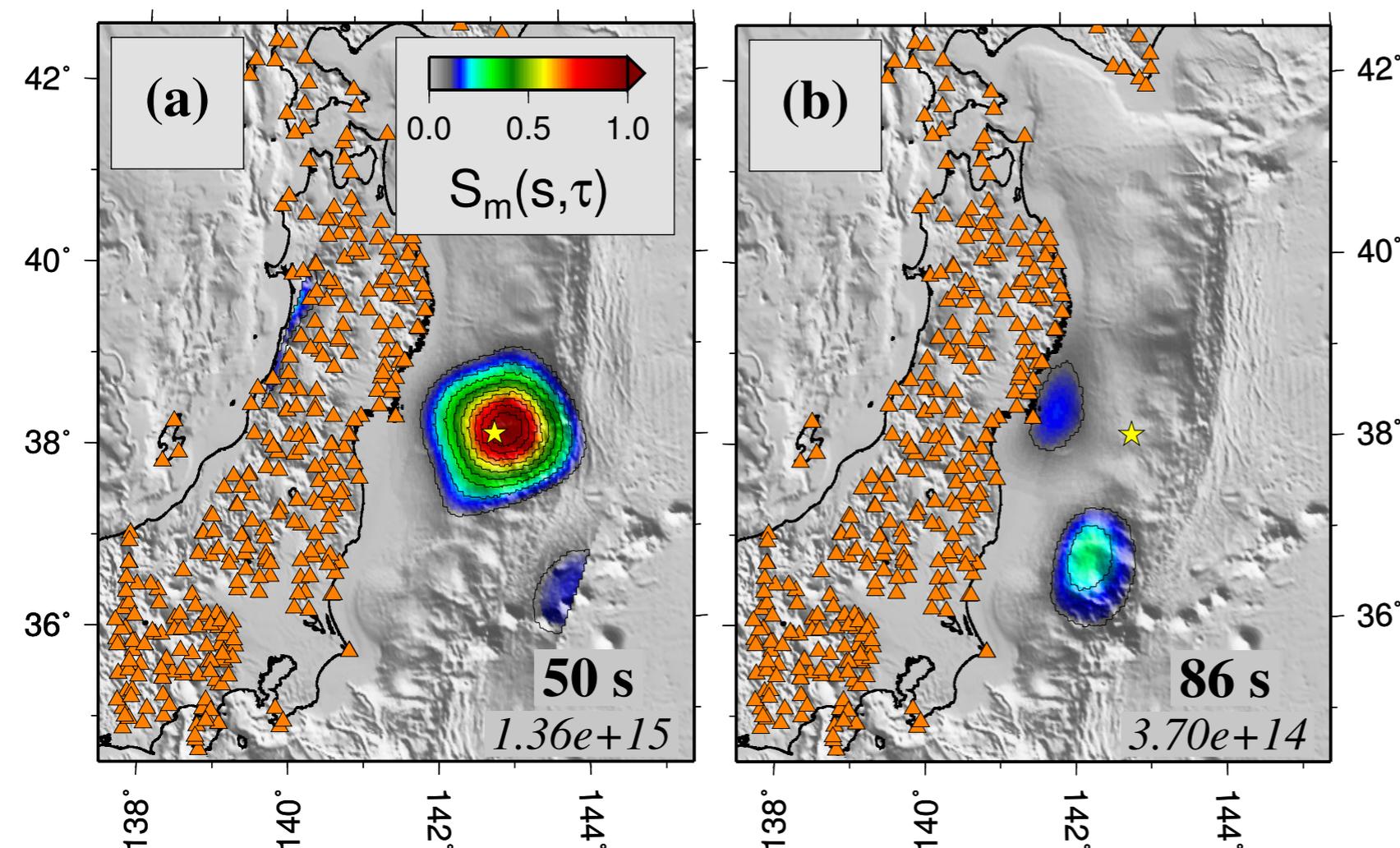
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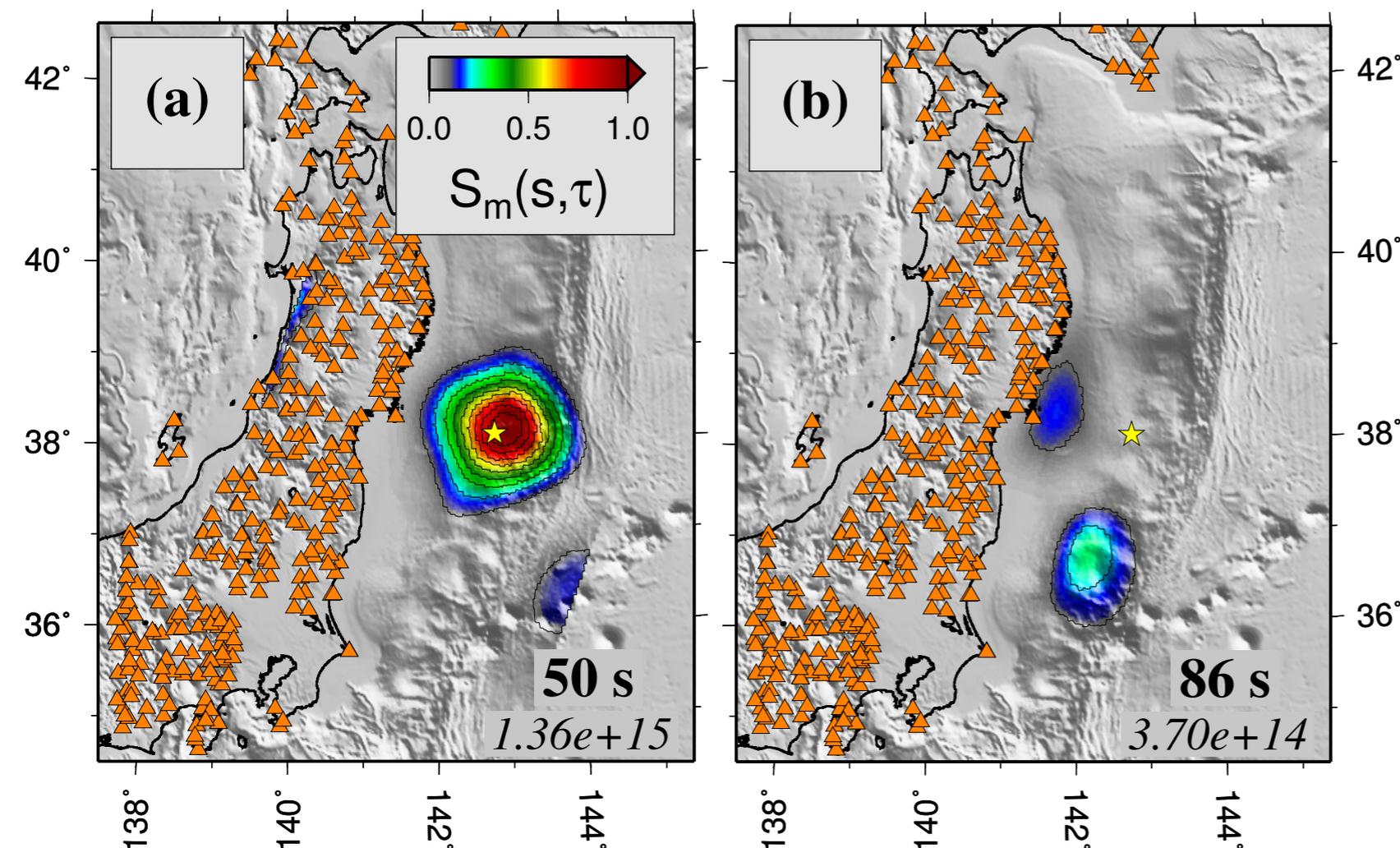
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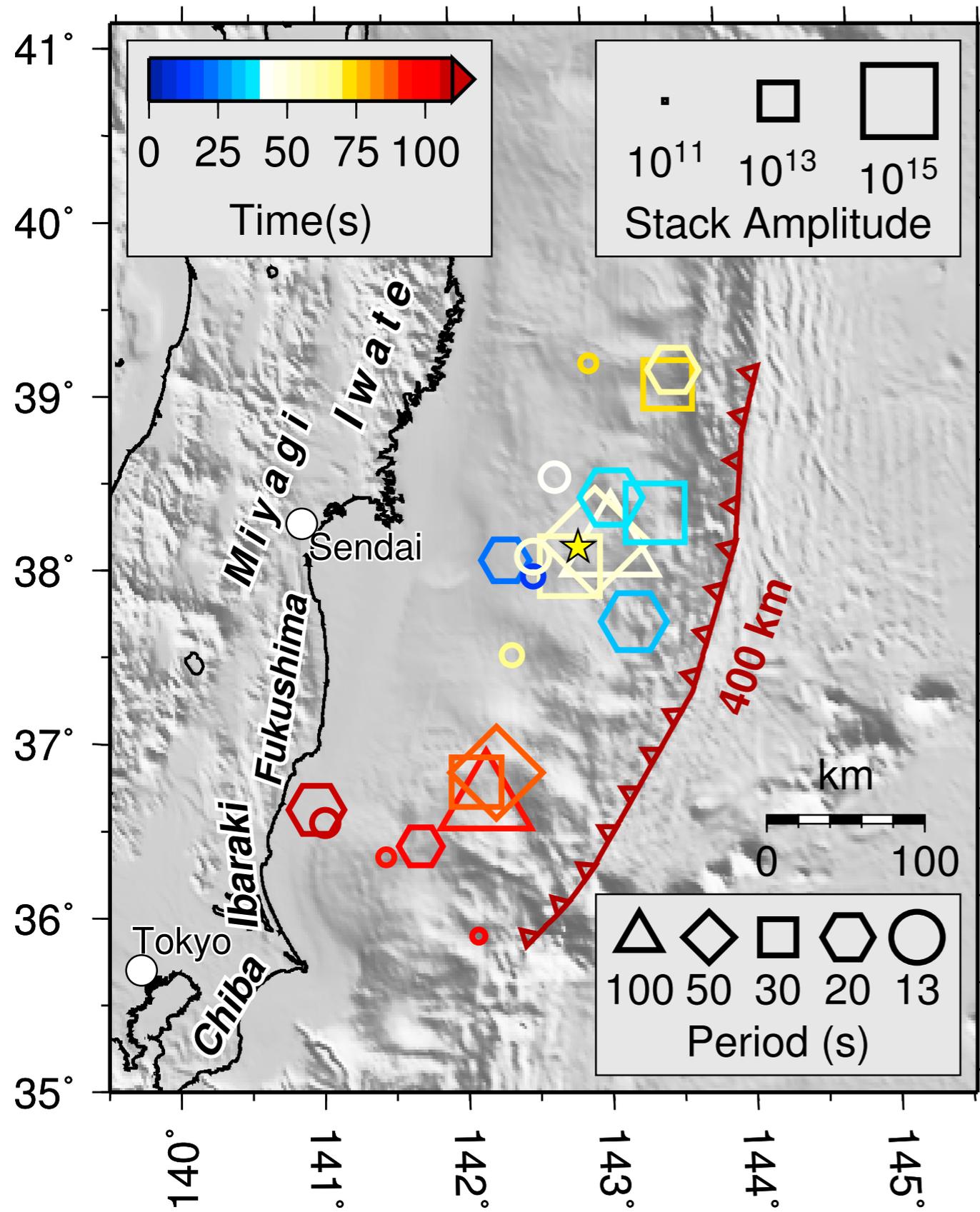
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# Application to the $M_w$ 9.1 mainshock



Authors select maxima of coherent ESE-WNW migrating peaks

**Stage 2** represents single broad peak at  $T=50, 100s$ ; at  $T=30s$  and shorter, two peaks are observed

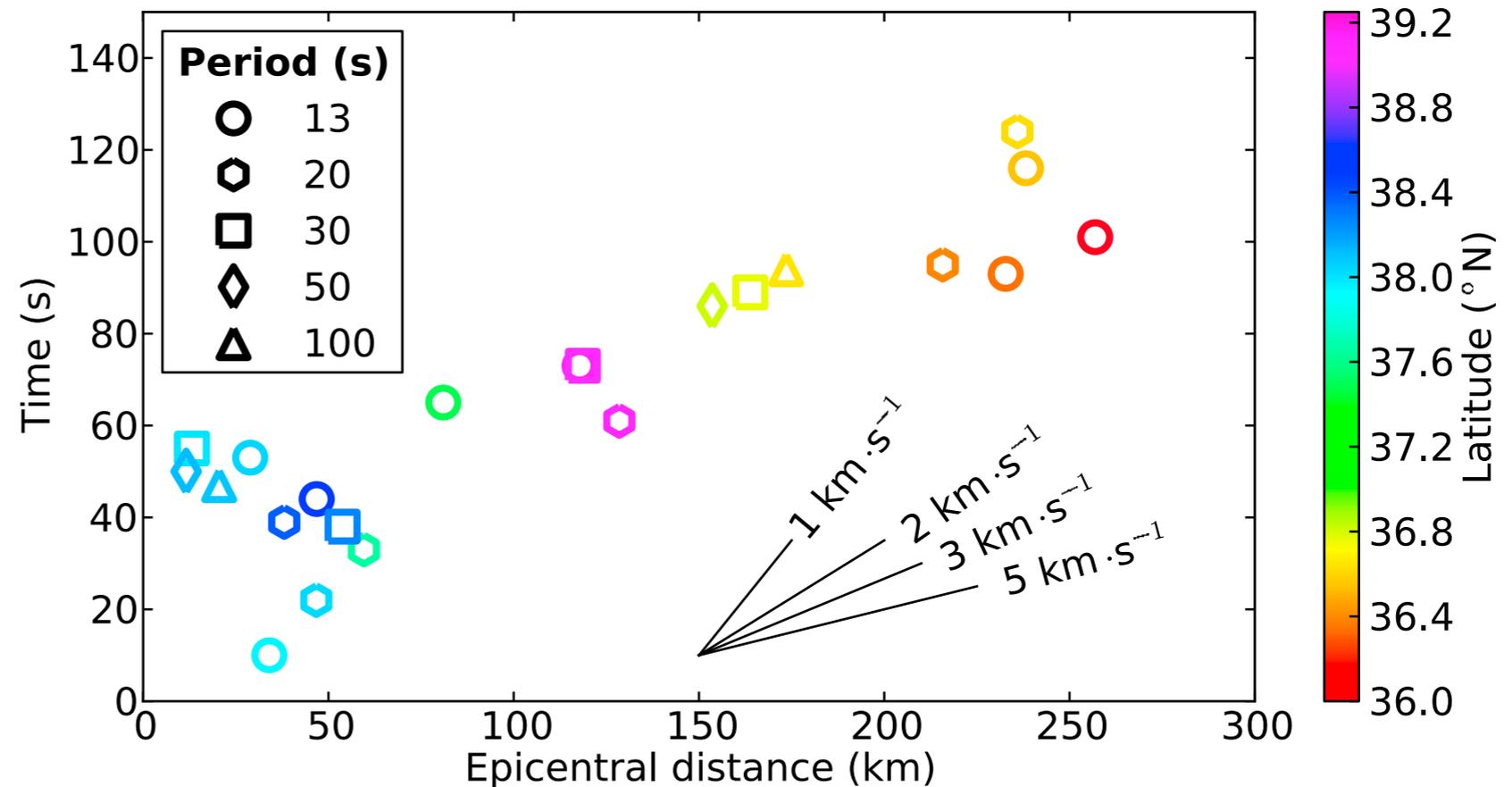
**Stage 3** northern segment visible *only* at  $T=30s$  and shorter

**Stage 3** southern segment visible at all periods; *single emitter* at  $T=30-100s$  while *second down-dip emitter* observed at  $T=13, 20s$

# Application to the $M_w$ 9.1 mainshock

Result: coarse, frequency-dependent view of rupture process

**Stage 1:** rupture down-dip at 2-3.5 km/s; potential up-dip component leading to Stage 2 at ~35 s;

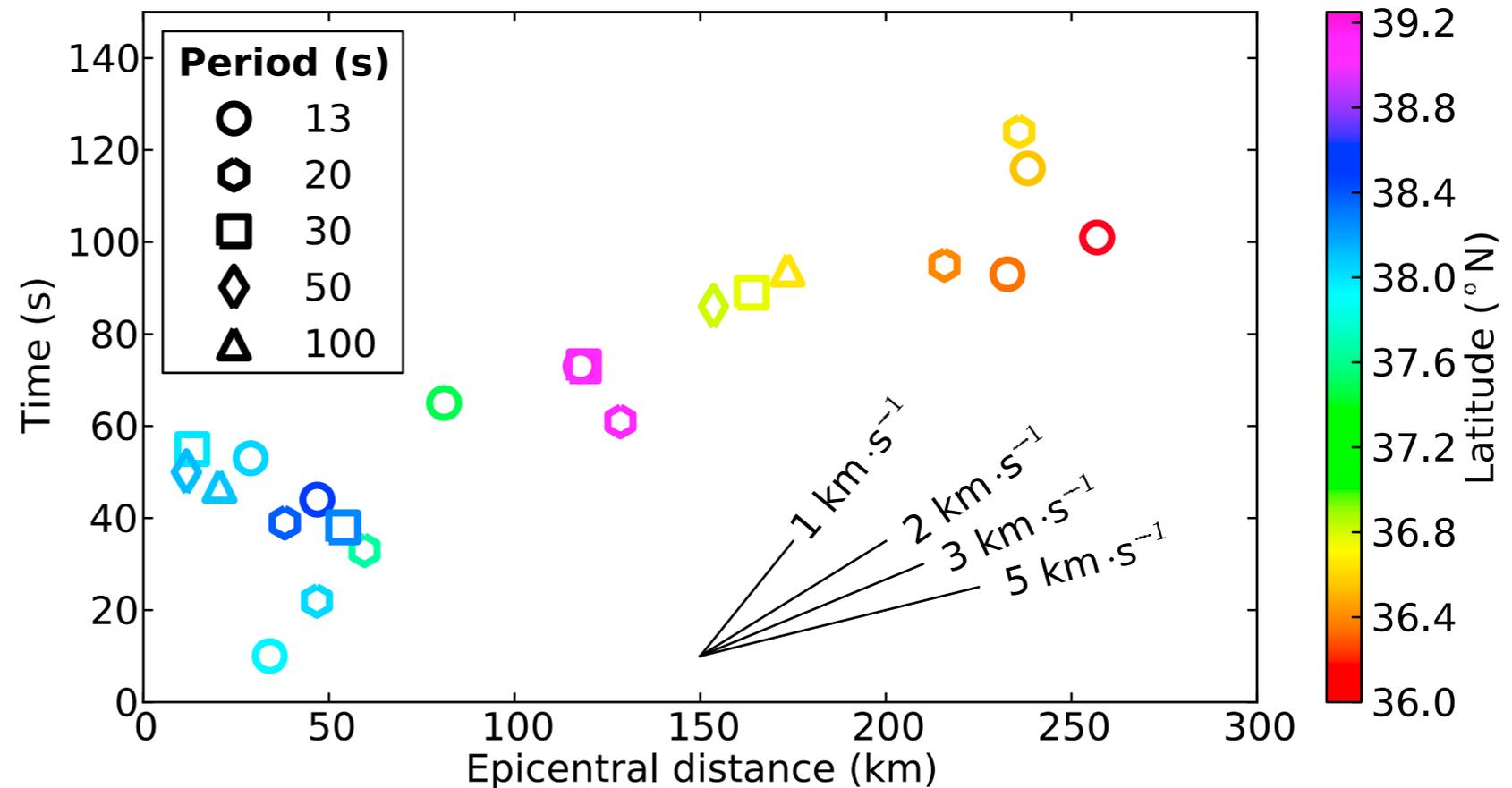


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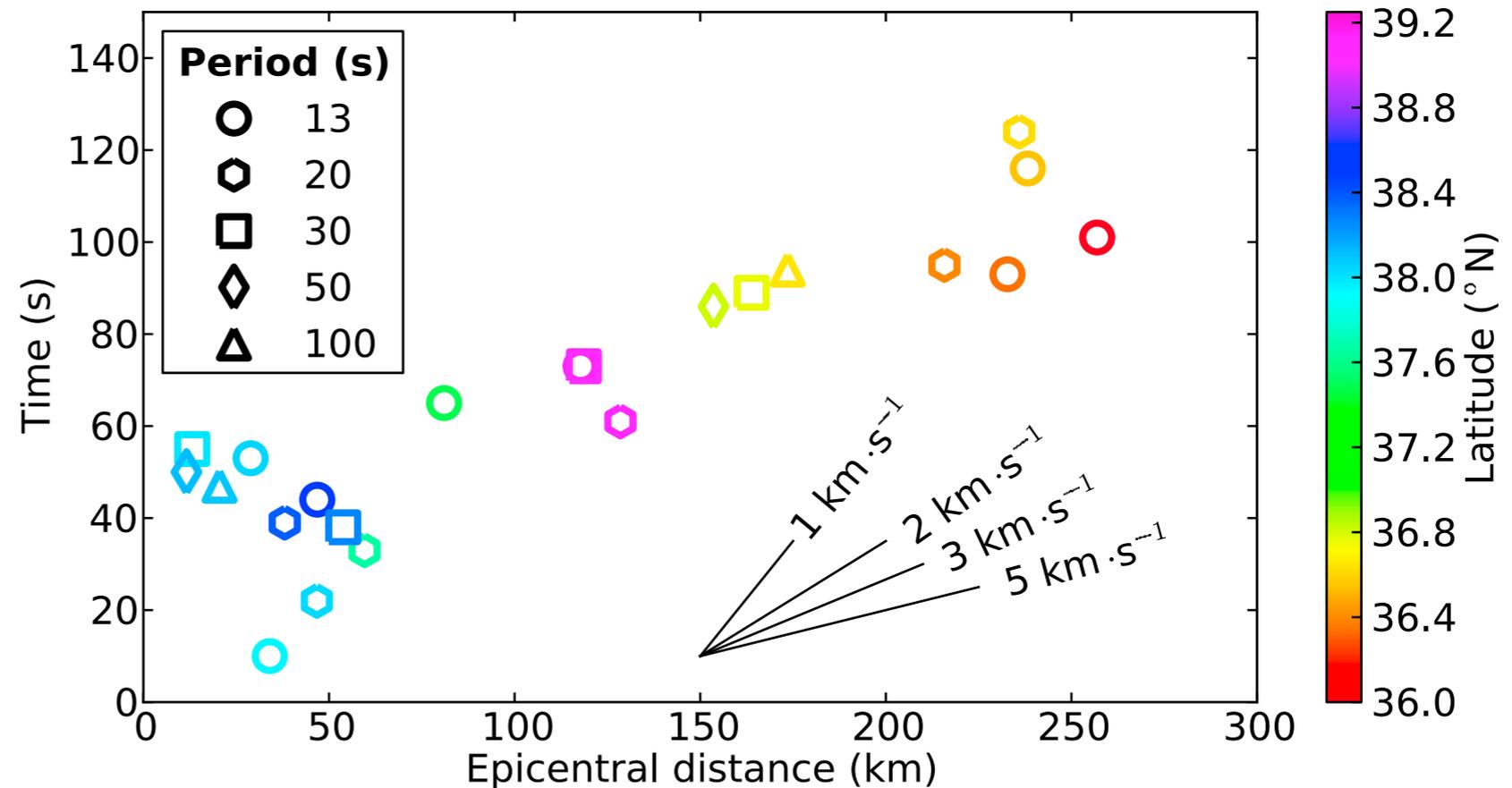
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**Stage 3:** *bilateral* - propagation to north off Iwate at  $\sim 60$  s (short period:  $T \leq 30$ s) and south off Fukushima-oki at 85-100 s. Inferred rupture velocity of 3-3.5 km/s; down-dip component at short periods ( $T \leq 20$ s) below Fukushima-oki at  $\sim 120$  s



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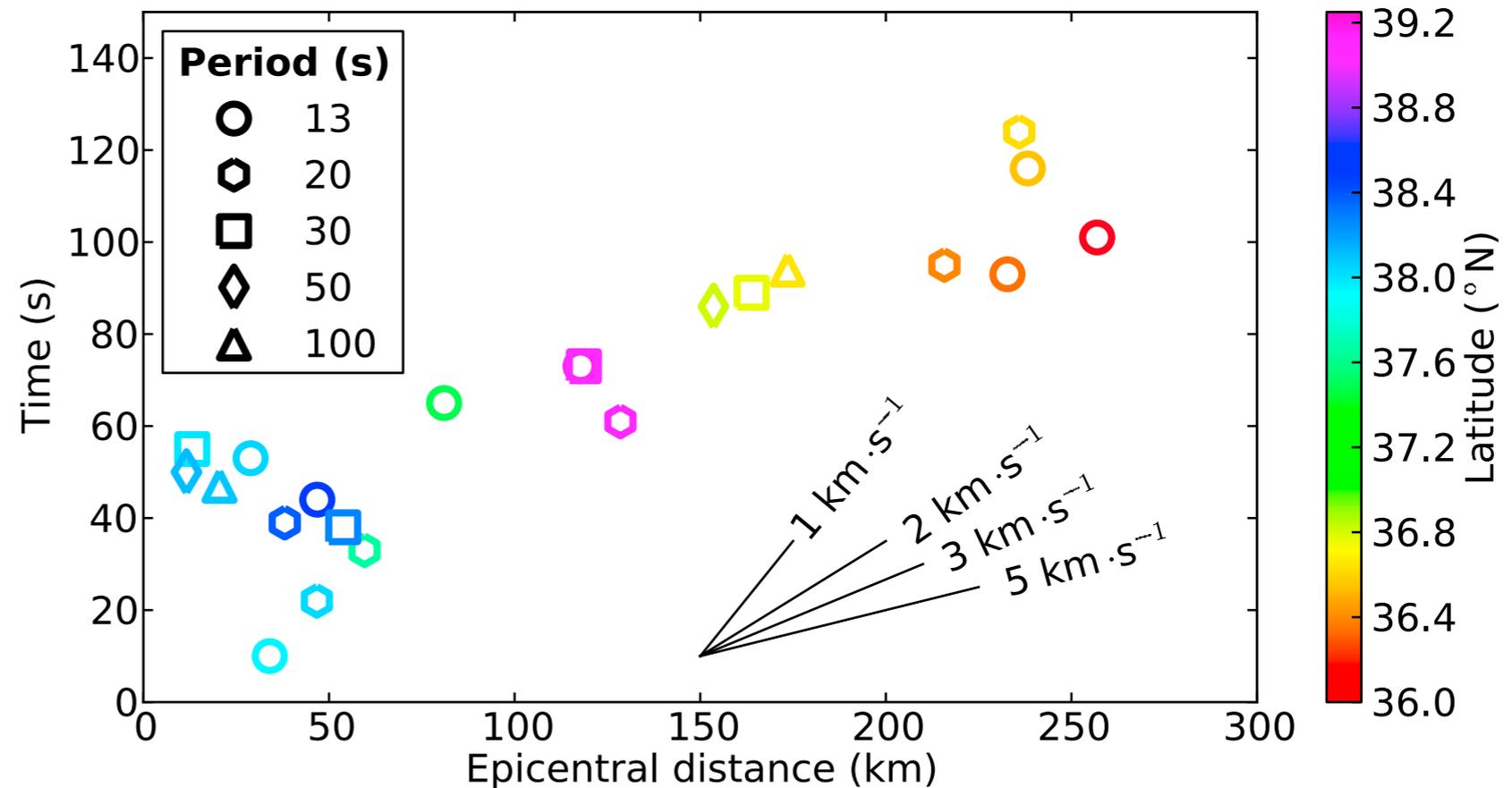
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*Total rupture along trench > 400km*

# Comparison with other studies

- Distribution of rupture broadly consistent with finite source models in other studies - particularly maximum slip near epicenter [e.g. Simons et al., 2011]
- Progression (three-stage: 1. weak; 2. strong; 3. bilateral rupture) also broadly consistent with others [e.g. Koketsu et al., 2011]
- Peak moment release in most studies at 60-80 s, while maximum BP amplitudes at 33-55 s (freq. dependent)
- Stage 3 bilateral rupture velocities faster than reported elsewhere: 3-3.5 km/s vs. 2.5 km/s [e.g. Koketsu et al., 2011]
- Stage 3 southern segment stronger than implied by long-period finite fault inversions - source directivity effect on BP? (synthetic experiment suggest this is possible)

*Majority of long-period emitters within 100 km of trench, unlike shorter-period BP studies - highlights frequency-dependent radiation effect [e.g. Koper et al., 2011]*

# Conclusions

- Provides novel method for studying megathrust earthquake rupture
- Inferred distribution of rupture consistent with other studies using a variety of methods (GPS, waveform, tsunami)
- Highlights effect of frequency-dependent seismic wave radiation
- Slip inferred near trench more consistent with studies including longer-period seismic and tsunami waveforms
- Method is low-resolution and limited by the azimuthal coverage of the array, but potentially valuable as it is inexpensive